**Performance Investigation of a Two Link Manipulator Stability in the Presence of Torque Disturbance using Optimal Sliding Mode Controller**

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**Abstract:** In this paper, a two-link manipulator system stability performance is designed and analyzed using Optimal control technique. The manipulator system is highly nonlinear and unstable. The system is modelled using Lagrangian equation and linearized in upward unstable position. The closed loop system is designed using optimal sliding mode controller. The system is compared with a known PID controller with an impulse applied and disturbance torques and a promising results has been obtained.

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**Keywords:** Manipulator, Sliding mode controller, Proportional integral derivative (PID) controller

1. **Introduction**

In robotics, a manipulator is a system used to manipulate items without any help by the operator. The stubbornness was originally for behavior with radioactive or biohazardous materials, using robotic arms, or they were used in inaccessible places. In more recent development they have been used in diverse pedestal of application including welding automation, robotic surgery and in space. It is an arm-like system that consists of a design of segments, usually sliding or jointed called cross-slides, which nelson and protocol aim with a amounts of degree of freedom. In industrial ergonomics a manipulator is a lift-assist contrivance used to help laborer lift, maneuver and position articles in tendency that are too heavy, too hot, too large or otherwise too difficult for a single worker to manually handle. As opposed to simply vertical lift assists (cranes, hoists, etc.) manipulators have the expertise to sweeps in to tight spaces and remove work pieces. A good form would be banishment large stamped parts from a press and arranging them in a rack or similar dunnage. In welding, a rods boom manipulator is used to reprieve ejection rates, reduce human inaccuracies and other costs in a manufacturing setting. Additionally, manipulator tooling gives the lift assist the aptitude to pitch, roll, or spin the parts for appropriate placement.

1. **System Description**

Figure 1 shows the physical model of a two-link manipulator, with each joint equipped with a motor for providing input torque disturbance, an encoder is used to measure the joint position. The objective of the of this system design is to make the joint positions to be stable to the vertical position with the presence of T1 and T2 disturbance inputs, which are specified by the vertical system design of the manipulator.

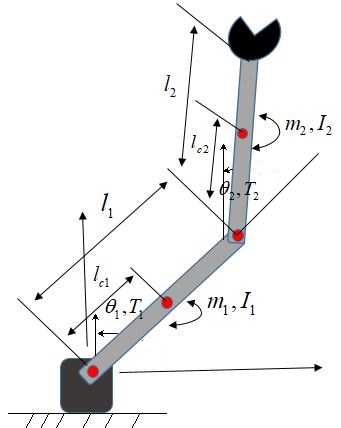


Figure 1. Vertically designed two link manipulator

By using the Lagrangian equations, one can easily show that the dynamic equations of the manipulator are



Where







Where

 Torque applied 1

 Torque applied 2

 Torque disturbance 1

 Torque disturbance 2

* 1. **Linearizing the System**

In this paper, the system linearizing method is done for vertical unstable equilibrium by taking.





Then Equation (2,3 and 4) becomes







Then Equation (1) becomes



Where





The parameters of the system are shown in Table 1 below.

|  |  |  |  |
| --- | --- | --- | --- |
| No | Parameter | Symbol | Value |
| 1 | Mass of the arm |  | 4 Kg |
| 2 | Mass of the wrist |  | 3 Kg |
| 3 | Length of the arm |  | 0.7 m |
| 4 | Length of center of mass of arm |  | 0.35 m |
| 5 | Length of the wrist |  | 0.6 m |
| 6 | Length of center of mass of wrist |  | 0.3 m |
| 7 | Moment of inertia of arm |  | 0.8 Kg m2/s2 |
| 8 | Moment of inertia of wrist |  | 0.6 Kg m2/s2 |
| 9 | Gravitational acceleration |  | 10 m/s2 |

The value of the matrix S, N and W becomes



The system equation becomes



Rearranging Equation (9) becomes



Let



So the state space representation of the system becomes



1. **The Proposed Controllers Design**
   1. **Optimal Sliding Mode Controller**

For the linear system



the objective is to minimize



subject to constraints



Here, the input term is not present in the objective function (16), and the constraints are that the system is on the intersection on *m* sliding hyperplanes. Furthermore, the matrix *G* is not specified *a priori* and will come out as a solution to the problem.

Using the similarity transformation



Where



If  then , then because the signs of eigenvalues are preserved under congruence transformation. Partition to conform to the partition of **q** in as follows:



Then, from (2),



When , the (*n*−*m*) dimensional dynamics is represented by



Equation 21 and Equation 22 constitute a standard LQ problem provided *R* > 0. If *Q* is chosen to be positive definite, *R* is guaranteed to be positive definite. In general, *R* is not guaranteed to be positive definite if *Q* is positive semidefinite. If *R* does not turn out to be positive definite, it has to be arbitrarily chosen to be a positive definite matrix. In this case, a new *Q* will be defined according to (19).

The gain matrix *K* for the minimum value of *J* is



Where



For this system the Q, R and N matrices are



The gain matrix K becomes



* 1. **PID Controller.**

A proportional-integral-derivative controller (PID) is a mechanism employing feedback that is widely used in industrial control organization and a variety of other implementation requiring continuously modulated control. A PID controller continuously calculates an inaccuracies values as the unlikeness between a desired set point (SP) and a measured process variable (PV) and applies a adjustment based on proportional, integral, and derivative terms (denoted P, I, and D respectively). In practical terms it automatically applies accurate and responsive change to a control function. The controller's PID algorithm restores the measured output to the desired input with minimal deferment and overshoot by increasing the ability of the system. The distinguishing feature of the PID controller is the skill to use the three control terms of proportional, integral and derivative pertinence on the controller output to apply accurate and optimal control.

The proportional, integral, and derivative terms are summed to calculate the output of the PID controller. Defining u (t) as the controller output, the final term of the PID controller is:

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* + 1. **Tuning**

The part of these effects is achieved by loop tuning to whip the optimal control function. The tuning constants are denoted as "K" and must be derived for each control application, as they depend on the response wood of the complete loop external to the controller. These are dependent on the behavior of the final control element.

Using Chien, Hrones and Reswick (CHR) PID Tuning Algorithm method the value of the PID controller are



1. **Result and Discussion**
   1. **Comparison of the Two Link Manipulator with Optimal Sliding Mode and PID Controllers for an Impulse Input Torque 1**

The simulation results of for the comparison of the two link manipulator with optimal sliding mode and PID controllers for an impulse input torque 1 of 0.1 Nm are shown in Figure 2 and Figure 3 respectively.

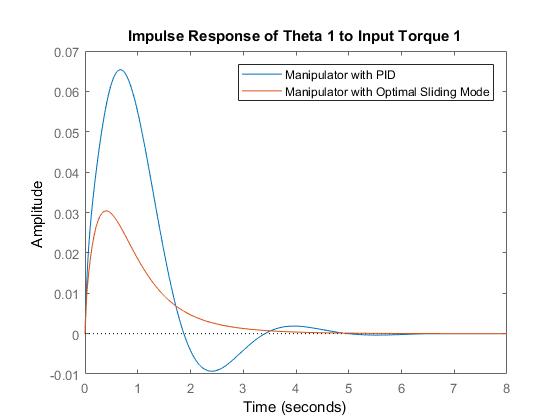


Figure 2. Impulse response of Theta 1 to Torque 1

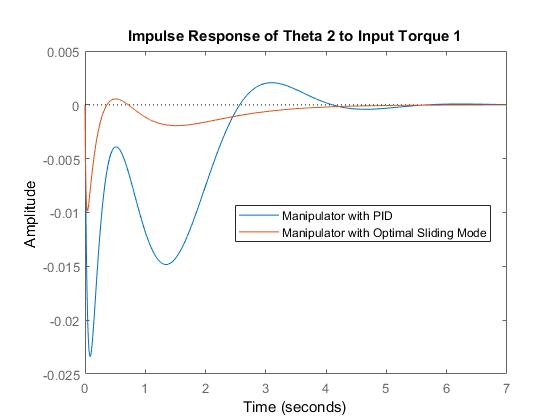


Figure 3. Impulse response of Theta 2 to Torque 1

The simulation result of the impulse response of theta 1 and theta 2 to torque 1 disturbance shows that the manipulator with optimal sliding mode controller minimizes the overshoot and the settling time better than the PID controller.

* 1. **Comparison of the Two Link Manipulator with Optimal Sliding Mode and PID Controllers for an Impulse Input Torque 2**

The simulation results of for the comparison of the two link manipulator with optimal sliding mode and PID controllers for an impulse input torque 2 of 0.1 Nm are shown in Figure 4 and Figure 5 respectively.

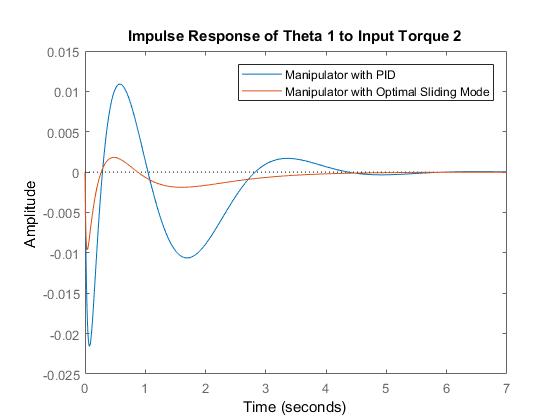


Figure 4. Impulse response of Theta 1 to Torque 2

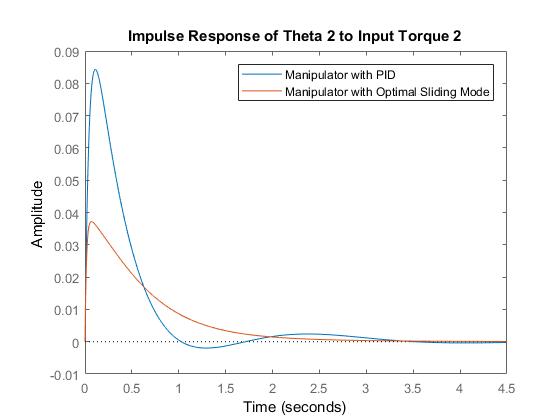


Figure 5 Impulse response of Theta 2 to Torque 2

The simulation result of the impulse response of theta 1 and theta 2 to torque 2 disturbance shows that the manipulator with optimal sliding mode controller minimizes the overshoot and the settling time better than the PID controller.

1. **Conclusion**

In this paper, stability control of a two link manipulator has been done using optimal sliding mode and proportional integral derivative controllers. The stability performance of the system has been analyzed using comparison simulation between the proposed controllers. The comparison simulation of the two link manipulator with optimal sliding mode and proportional integral derivative controllers has been done for an impulse input of the applied and disturbance torques and the simulation results prove the effectiveness of the proposed optimal sliding mode controller in minimizing the overshoot with a moderate settling time better than the proportional integral derivative controller.

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