



Modelling Design and Control of an Electromechanical Mass Lifting System using Optimal and Robust control Method

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Abstract: In this paper, an electromechanical mass lifter system is designed, analyzed and compare using optimal and robust control theories. LQR and μ -synthesis controllers are used to improve the lift displacement by comparison method for tracking the desired step and sinusoidal wave signals input. Finally, the comparison simulation result prove the effectiveness of the electromechanical mass lifter system with μ -synthesis controller for improving the rise time, percentage overshoot, settling time and peak value of tracking the desired step displacement signal and improving the peak value for tracking the desired sinusoidal displacement signal with a good performance.

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1. Introduction

In engineering, electromechanical systems combines strategies and tactics drawn from electrical engineering and mechanical engineering. Electromechanical systems specializes in the interaction of electrical and mechanical systems as an entire and how the two structures interact with every different. This manner is especially distinguished in systems such as those of DC or AC rotating electric machines which may be designed and operated to generate energy from a mechanical system (generator) or used to strength a mechanical impact (motor). Electrical engineering in this context additionally encompasses electronics engineering. Electromechanical systems are ones which have each electrical and mechanical processes. It operated by hand switch is an electromechanical element due to the mechanical movement causing an electrical output. Though this is proper, the term is normally understood to consult system which contain an electrical signal to create mechanical motion, or vice versa mechanical motion to create an electric signal. Often involving electromagnetic standards such as in relays, which permit a voltage or cutting-edge to manipulate every other, normally remoted circuit voltage or contemporary by means of robotically switching units of contacts, and solenoids, via which a

voltage can actuate a moving linkage as in solenoid valves.

2. Mathematical Model

The electromechanical mass lifter system is shown in Figure 1 below.

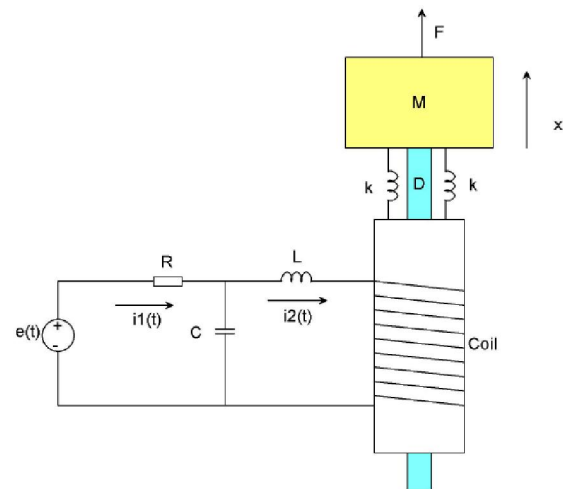


Figure 1 Electromechanical mass lifter system

For a simplified analysis assume that the coil has

a back emf of $e_b = k_b \frac{dx}{dt}$ and the coil current

produce a force $F_c = k_f i(t)$ on the mass M. For the electrical circuit applying KVL for loop 1 & 2 yields:

Loop 1

$$e(t) = Ri_1(t) + \frac{1}{C} \int (i_1(t) - i_2(t)) dt$$

Taking Laplace transform

$$E(s) = RI_1(s) + \frac{1}{sC} I_1(s) - \frac{1}{sC} I_2(s) \quad (1)$$

Loop 2

$$e_b(t) = L \frac{di_2(t)}{dt} + \frac{1}{C} \int (i_2(t) - i_1(t)) dt$$

Taking Laplace transform

$$E_b(s) = sLI_2(s) + \frac{1}{sC} I_2(s) - \frac{1}{sC} I_1(s) \quad (2)$$

The plunger moves because of the electromagnetic force generated when a current $i_2(t)$ passes through the coil a back emf is generated in the coil (Lenz law) is given by:

$$e_b(t) = k_b \frac{dx}{dt}$$

Taking Laplace transform

$$\frac{X(s)}{E(s)} = \frac{k_f}{\left[RLCMs^4 + L(M + RCD)s^3 + [RM + LD + RC(2Lk + k_f k_b)]s^2 + (RD + 2Lk + k_f k_b)s + 2Rk\right]}$$

The parameters of the electromechanical system is shown in Table 1 below:

No	Parameter	Symbol	Value
1	Resistor	R	10 ohm
2	Inductor	L	5 H
3	Capacitor	C	0.001 F
4	Mass	M	55 Kg
5	Spring Stiffness	K	100 N/m
6	Damper	D	10 N-s/m
6	Lenz constant	k_b	13
7	Force constant	k_f	32

The electromechanical mass lifter system transfer function is

$$\frac{X(s)}{E(s)} = \frac{32}{0.015s^4 + 2s^3 + 63s^2 + 1516s + 2000}$$

The state space representation of the system is

$$E_b(s) = sk_b X(s) \quad (3)$$

When a current $i_2(t)$ flows through the coil a mechanical force is developed which is given by:

$$F(t) = k_f i_2(t)$$

Taking Laplace transform

$$F(s) = k_f I_2(s) \quad (4)$$

Where

k_f Is the force constant N/A

For the mass system

$$F(t) = M \frac{d^2x}{dt^2} + D \frac{dx}{dt} + 2kx$$

Taking Laplace transform and rearrange

$$F(s) = [s^2M + sD + sk] X(s) \quad (5)$$

Substituting Eqn (1) into Eqn (2) for $i_1(t)$ and substituting Eqn (3) into the modified Eqn (2) and substituting Eqn (2) into Eqn (4) and finally substituting the modified Eqn (4) into Eqn (5) yields the transfer function the input voltage and the output displacement as:

$$\dot{x} = \begin{pmatrix} -130 & -4200 & -101070 & -133330 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} + \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} u$$

$$y = (0 \ 0 \ 0 \ 2133.3) \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix}$$

3. The Proposed Controllers Design

In this section, the design of the electromechanical mass lifter system with μ -synthesis and LQR controllers is done respectively.

3.1 μ -Synthesis Controller Design

The electromechanical mass lifter system with μ -synthesis controller block diagram is shown in Figure 2.

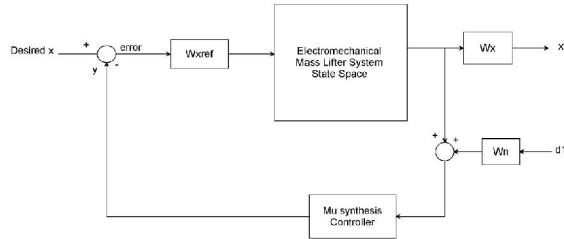


Figure 2 Electromechanical mass lifter system with μ - synthesis controller system interconnections block diagram

A μ -synthesis controller is synthesized the use of D-K generation. The D-K generation method is an approximation to synthesis that tries to synthesize the controller. There is one manage input the preferred stage signal. There are two purposes for the weighted function norm: for a given norm, there might be a right away evaluation for remarkable performance objectives and they may be used for knowledge the frequency facts integrated into the evaluation. The output or feedback signal y is

$$y = (x + d_1 \times W_n)$$

The controller's acts at the y signal to provide the remarks displacement signal. The W_n block modelled the disturbance in the channel. W_n is given a disturbance noise of 0.04m.

$$W_n = 0.04$$

W_n is used to model the noise of the displacement sensor. The value of the error disturbance is scaled the use of the weight W_{xref} . Let us anticipate the maximum error disturbance is 0.08 m because of this

$$W_{xref} = 0.08$$

The weighting function W_x are used to keep the output displacement over the desired range. The water level W_{h1} is given as

$$W_x = \frac{1}{s + 3}$$

The resulted μ -synthesis controller is

$$K_\mu = \frac{s + 25}{s^2 + 155s + 256}$$

3.2 LQR Controller

LQR is a manage system that gives the fine viable overall performance with apprehend to some given degree of usual performance. The normal performance degree is a quadratic characteristic composed of state vector and control input.

Linear Quadratic Regulator (LQR) is the handiest concept of pole placement technique. LQR set of guidelines defines the most excellent pole location based on two cost function. To find out the

most fulfilling profits, one have to outline the most beneficial performance index first off after which resolve algebraic Riccati equation. LQR does not have any particular approach to define the cost function to benefit the most appropriate profits and the value feature must be described in iterative way.

LQR is a manipulate scheme that offers the outstanding viable common overall performance with respect to a few given degree of overall performance. The LQR design problem is to design a state feedback controller K such that the objective function J is minimized. In this technique a feedback gain matrix is designed which minimizes the objective function an excellent way to benefit some compromise a number of the usage of manage attempt, the importance, and the speed of reaction at the manner to assure a stable system. For a continuous-time linear system defined by using

$$\dot{x} = Ax + Bu \quad (6)$$

With a cost functional defined as

$$J = \int (x^T Qx + u^T Ru) dt \quad (7)$$

Where Q and R are the weight matrices, Q is required to be high quality precise or high quality semi-definite symmetry matrix. R is required to be positive definite symmetry matrix. One practical method is to Q and R to be diagonal matrix. The value of the factors in Q and R is related to its contribution to the cost function J . The feedback manage regulation that minimizes the value of the cost is:

$$u = -Kx \quad (8)$$

K is given by

$$K = R^{-1} B^T P \quad (9)$$

And P can be located through solving the continuous time algebraic Riccati equation:

$$A^T P + PA - PBR^{-1} B^T P + Q = 0 \quad (10)$$

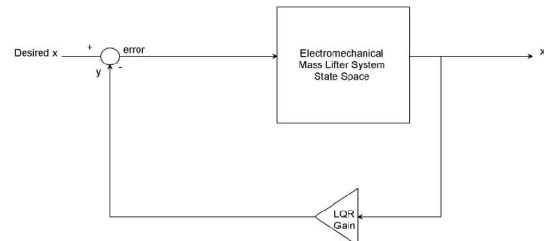


Figure 3. State variable feedback configuration By taking

The value of weighted matrix Q (country variable) and R (control variable) is based upon on designer. Designer pick out the right cost of Q and R to discover the perfect advantage matrix K the usage

of MATLAB. The State variable feedback configuration is shown below in Figure 3.

$$Q = \begin{bmatrix} 5 & 0 & 0 & 0 \\ 0 & 5 & 0 & 0 \\ 0 & 0 & 5 & 0 \\ 0 & 0 & 0 & 5 \end{bmatrix} \text{ And } R=1$$

The value of obtained feedback gain matrix K of LQR is given by

$$K = [0.0023 \ 0.0581 \ 0.0766 \ 0.0000]$$

4. Result and Discussion

Here in this section, the comparison of the electromechanical mass lifter system with μ -synthesis and LQR controllers for tracking the desired output displacement using a step and sinusoidal wave signals.

4.1 Comparison of the electromechanical mass lifter system with μ -synthesis and LQR controllers for a Desired Step Displacement Signal

The Simulink model for the electromechanical mass lifter system with μ -synthesis and LQR controllers for a desired step displacement signal is shown in Figure 4 below.

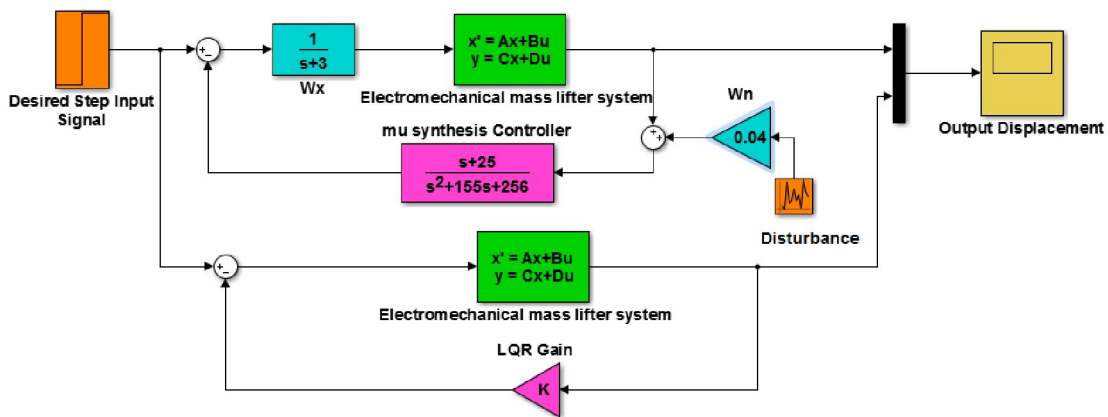


Figure 4 Simulink model for the electromechanical mass lifter system with μ -synthesis and LQR controllers for a desired step displacement signal

The simulation result of the comparison of the electromechanical mass lifter system with μ -synthesis and LQR controllers for a desired step displacement signal is shown in Figure 5 below.

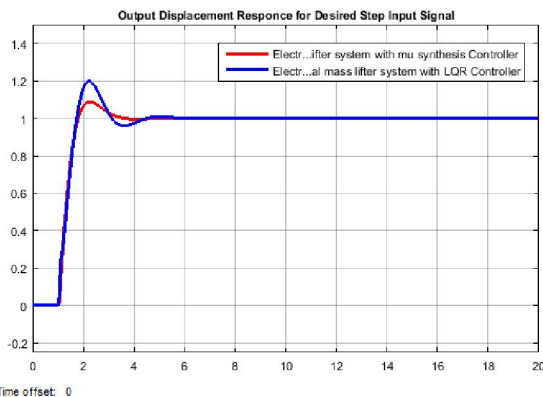


Figure 5. Simulation result of the comparison of the electromechanical mass lifter system with μ -synthesis and LQR controllers for a desired step displacement signal

The tank system with the proposed controllers Performance specification is shown in Table 2 below.

Table 2. Performance measurement of a step response

No	Performance measure	μ -synthesis	LQR
1	Rise time	1.12 sec	1.2 sec
2	Percentage Overshoot	9.09 %	16.66 %
3	Settling time	4 sec	5.8 sec
4	Peak value	1.1 m	1.21 m

Table 2 shows that the electromechanical mass lifter system with μ -synthesis improve the rise time, percentage overshoot, settling time and peak value for tracking the desired step displacement signal with a good performance.

4.2 Comparison of the electromechanical mass lifter system with μ –synthesis and LQR controllers for a Desired Sinusoidal Displacement Signal

The Simulink model for the electromechanical mass lifter system with μ –synthesis and LQR controllers for a desired step displacement signal is shown in Figure 6 below.

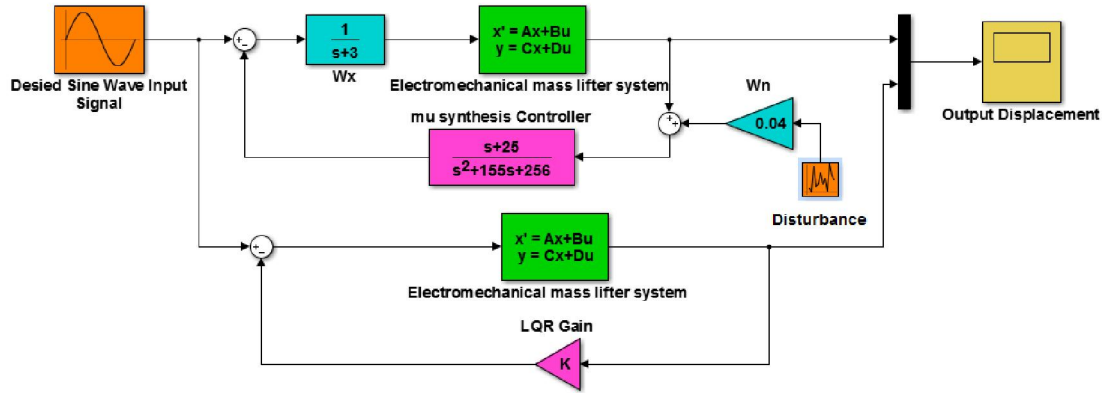


Figure 6. Simulink model for the electromechanical mass lifter system with μ –synthesis and LQR controllers for a desired sinusoidal displacement signal

The simulation result of the comparison of the electromechanical mass lifter system with μ –synthesis and LQR controllers for a desired sinusoidal displacement signal is shown in Figure 7 below.

Table 3 shows that the electromechanical mass lifter system with μ –synthesis improve the peak value for tracking the desired sinusoidal displacement signal with a good performance.

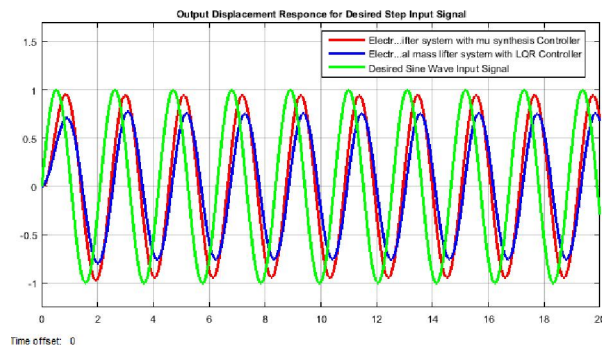


Figure 7. Simulation result of the comparison of the electromechanical mass lifter system with μ –synthesis and LQR controllers for a desired sinusoidal displacement signal

Table 3 Numerical peak values of the desired sinusoidal displacement signal simulation output

No	Systems	Peak value
1	Desired Input signal	1 m
2	μ –synthesis	0.97 m
3	LQR	0.7 m

5. Conclusion

In this paper, modelling, design, analysis and control of the electromechanical mass lifter system with μ –synthesis and LQR controllers is done with the aid of Matlab/Simulink Toolbox. The proposed controllers are compared for the mass lifting mechanisms by improving the performance of the system to track the desired mass lift displacement. Step and sinusoidal signals are used as a desired displacement signals to be tracked by the system. The electromechanical mass lifter system with μ –synthesis controller improve the performance of the system by 90.1 % for the desired step displacement input and 97 % for the desired sinusoidal displacement input. Finally, the comparison simulation result prove the effectiveness of the electromechanical mass lifter system with μ –synthesis controller.

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