



## Comparison of Mixed H<sub>2</sub>/H<sub>∞</sub> with Regional Pole Placement Control and H<sub>2</sub> Optimal Control for the Design of Steam Condenser

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**Abstract:** this paper considers the trouble of the usage of approximate strategies for realizing the neural controllers for nonlinear SISO systems. In this paper, we introduce the nonlinear autoregressive moving average (NARMA-L2) model which might be approximations to the NARMA model. The nonlinear autoregressive moving average (NARMA-L2) model is an precise illustration of the input–output behavior of finite-dimensional nonlinear discrete time dynamical systems in a neighborhood of the equilibrium state. However, it isn't always handy for purposes of neural networks due to its nonlinear dependence on the manipulate input. In this paper, nerves system based arm position sensor device is used to degree the precise arm function for nerve patients the use of the proposed systems. In this paper, neural network controller is designed with NARMA-L2 model, neural network controller is designed with NARMA-L2 model system identification based predictive controller and neural network controller is designed with NARMA-L2 model based model reference adaptive control system. Hence, quite regularly, approximate techniques are used for figuring out the neural controllers to conquer computational complexity. Comparison were made among the neural network controller with NARMA-L2 model, neural network controller with NARMA-L2 model system identification based predictive controller and neural network controller with NARMA-L2 model reference based adaptive control for the preferred input arm function (step, sine wave and random signals). The comparative simulation result shows the effectiveness of the system with a neural network controller with NARMA-L2 model based model reference adaptive control system.

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**Keywords:** Nonlinear autoregressive moving average, neural network, Model reference adaptive control, Predictive controller

### I. Introduction

The neural network pattern tins be used in dominion strategies that require a global creation of the diagram forward or inverse dynamics, and these form are available in the example of neural networks, which have been trained using neural based design discovery techniques. The generalized teaching dresser attempts to crops the inverse of a fortification over the entire kingdom crack using off-line training while in the specialized configuration the convention is on-line and uses incorrectness back dispersal through the movement to learn the protocol inverse liveliness over a small operating region. The global firmness of the closed-loop response design is guaranteed provided the arrangement of the robot-manipulator action phrase is exact. Generalization of the director over the desired path breach has been established using an on-line weight education scheme.

The advantage of a neuron-adaptive hybrids mastery scheme is the high accuracy and computationally less intensive proficiency scheme.

### II. System Discription

#### A. Nerves System Based Arm Position Sensor System Description

Nerves system based arm position sensor is a device which senses the electrical pulse signal of the nerve and compares the desired arm position and response arm position of the nerve defected arm. Nerves system based arm position sensor is a type of neuro modulation therapy in which electrodes are surfacely placed next to a selected peripheral nerve considered to be the source of nerve pain. One way of trying to control the arm position is that arises from peripheral nerves calls for a device that sends low levels of electricity to stimulate part (s) of the nerve. This electrical voltage is thought to interfere with how

the nerve transmits the voltage impulse signals and response through arm motion.

The mathematical description of the system is shown below.

$$\frac{d^2y(t)}{dt^2} = -\gamma + \frac{\alpha v^2(t)}{s y(t)} - \frac{\beta dy(t)}{s dt} \quad (1)$$

Where

$y(t)$  Arm position output

$v(t)$  Impulse voltage input

$\gamma$  Arm position acceleration

$s$  Device sensitivity function

$\alpha$  Nerve transmission coefficient

$\beta$  Nerve delay coefficient

The block diagram of the nerves system based arm position sensor device is shown in Figure 1 below.

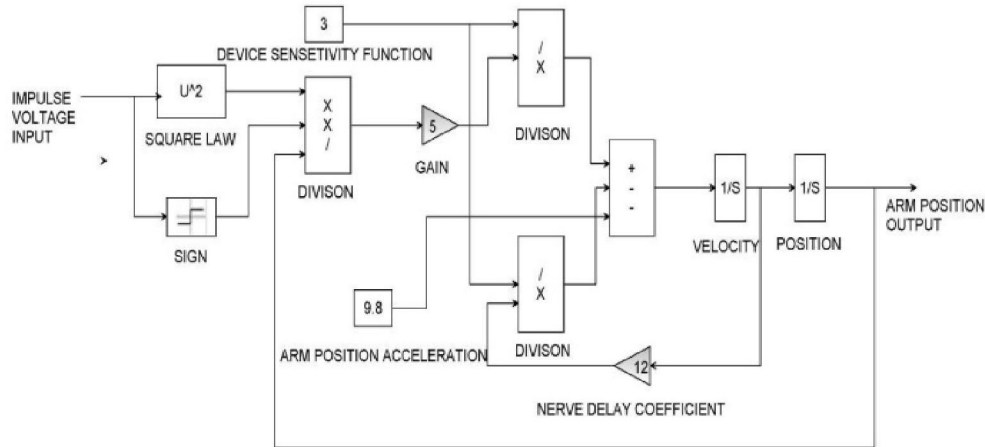


Fig. 1. Block diagram of the nerves system based arm position sensor device

### B. Design of NARMA-L2 Neural Network Controller

The neuro controller described on this phase is cited through two different names: response linearization control and NARMA-L2 manipulate. It is known as comments linearization when the plant shape has a specific form (associate form). It is known as NARMA-L2 manipulate while the fortification mold may be approximated by using the same form. The vital principle of this type of control is to convert nonlinear design system into linear dynamics with the aid of canceling the nonlinearities. This phase starts off evolved with the aid of submitting the associate system form and presentation how you may use a

neural community to become aware of this model. Then it describes how the identified neural network model may be used to broaden a controller.

1) *Identification of the NARMA-L2 Model:* The first step in the use of feedback linearization (or NARMA-L2) manipulate is to identify the design to be controlled. You train a neural network to represent the forward dynamics of the system.

The first step is to pick out a styles association to use. One standard patterns this is used to symbolize fashionable discrete-time nonlinear system is the nonlinear autoregressive-moving average (NARMA) model:

$$y(k+d) = N[y(k), y(k-1), \dots, y(k-n+1), u(k), u(k-1), \dots, u(k-n+1)] \quad (2)$$

Where  $u(k)$  is the system input, and  $y(k)$  is the system output. For the identification section, you can teach a neural network to approximate the nonlinear

function  $N$ . If you want the system output to follow some reference trajectory  $y(k+d) = y_r(k+d)$  the subsequent step is to expand a nonlinear controller of the form:

$$u(k) = G[y(k), y(k-1), \dots, y(k-n+1), y_r(k+d), u(k-1), \dots, u(k-m+1)] \quad (3)$$

The trouble with the usage of this controller is that in case you need to teach a neural network to

create the characteristic G to minimize mean square blunders, you need to apply dynamic returned propagation. This can be pretty sluggish. One answer

is to apply approximate models to symbolize the system. The controller used on this section is based totally at the NARMA-L2 approximate model:

$$\hat{y}(k+d) = f \left[ \begin{matrix} y(k), y(k-1), \dots, \\ y(k-n+1), u(k-1), \dots, u(k-m+1) \end{matrix} \right] + g \left[ \begin{matrix} y(k), y(k-1), \dots, y(k-n+1), \\ u(k-1), \dots, u(k-m+1) \end{matrix} \right] u(k) \quad (4)$$

This model is in associate shape, wherein the next controller input u (k) is not contained in the nonlinearity. The gain of this form is that you could

resolve for the control input that causes the system output to comply with the reference  $y(k+d) = y_r(k+d)$ . The resulting controller would have the form.

$$u(k) = \frac{y_r(k+d) - f(y(k), y(k-1), \dots, y(k-n+1), u(k-1), \dots, u(k-n+1))}{g[y(k), y(k-1), \dots, y(k-n+1), u(k-1), \dots, u(k-n+1)]} \quad (5)$$

Using this equation immediately can motive awareness problems, due to the fact you ought to

determine the control input u (k) primarily based on the output at the same time, y (k). So, rather, use the model.

$$y(k+d) = f \left[ \begin{matrix} y(k), y(k-1), \dots, y(k-n+1), \\ u(k-1), \dots, u(k-m+1) \end{matrix} \right] + g \left[ \begin{matrix} y(k), y(k-1), \dots, y \\ (k-n+1), u(k-1), \dots, u(k-m+1) \end{matrix} \right] u(k+1) \quad (6)$$

Where  $d \geq 2$ . Figure 2 shows the structure of a neural network representation.

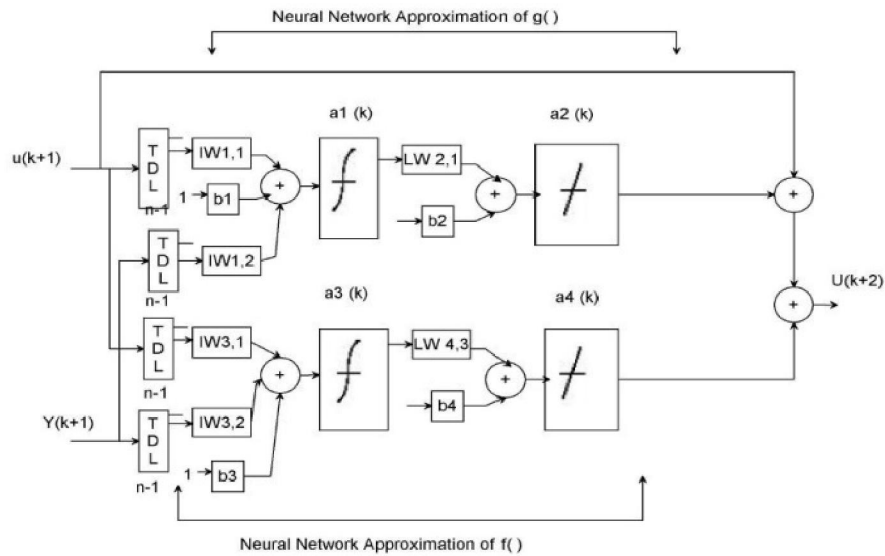


Fig. 2. The structure of a neural network representation.

Using the NARMA-L2 model, you can obtain the controller.

$$u(k+1) = \frac{y_r(k+d) - f(y(k), y(k-1), \dots, y(k-n+1), u(k), \dots, u(k-n+1))}{g[y(k), y(k-1), \dots, y(k-n+1), u(k), \dots, u(k-n+1)]} \quad (7)$$

Which is realizable for  $d \geq 2$ . Figure 3 shows the block diagram of the NARMA-L2 controller.

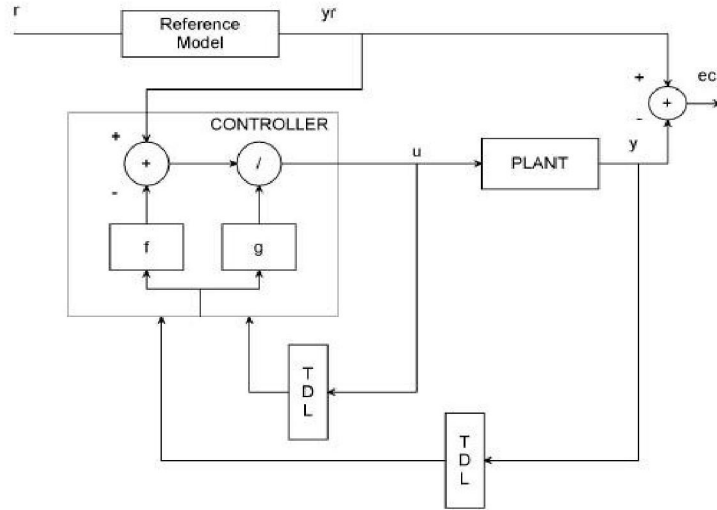


Fig. 3. Block diagram of the NARMA-L2 controller

This controller can be implemented with the formerly diagnosed NARMA-L2 plant model, as shown in Figure 4 below.

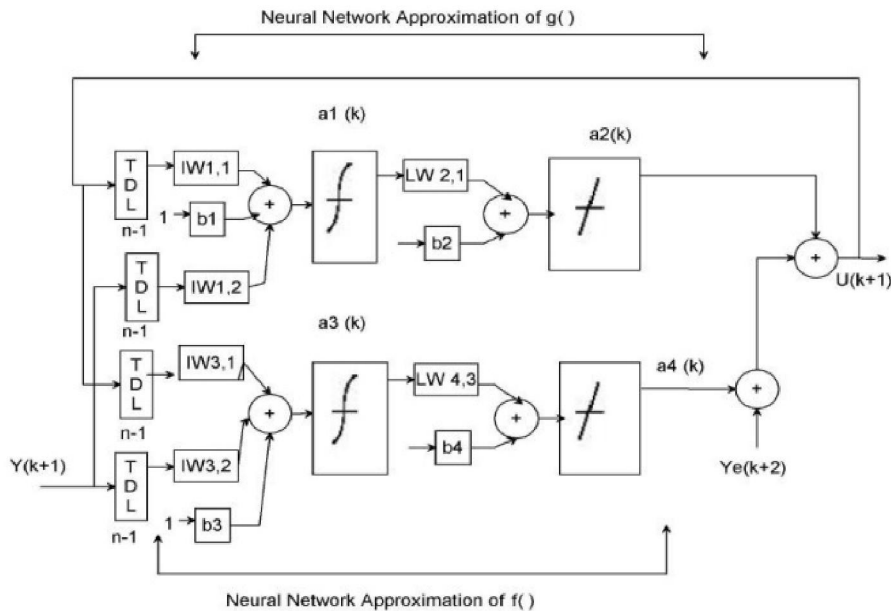


Fig. 4. Previously identified NARMA-L2 plant model

*C. Design of NARMA-L2 Model Controller Using System Identification*

The NARMA-L2 based neural network predictive controller makes use of a neural network model of a nonlinear plant to expect future plant performance. The controller then calculates the control input that will optimize plant performance over a targeted destiny time horizon. The first step in model predictive control is to determine the neural

network plant model. Next, the plant model is utilized by the controller to predict future performance.

*1) System Identification:*

The first stage of model NARMAL2 based predictive controller is to train a neural network to symbolize the ahead dynamics of the plant. The prediction errors among the plant output and the neural network output is used as the neural network

education signal. The method is shown in Figure 5 below:

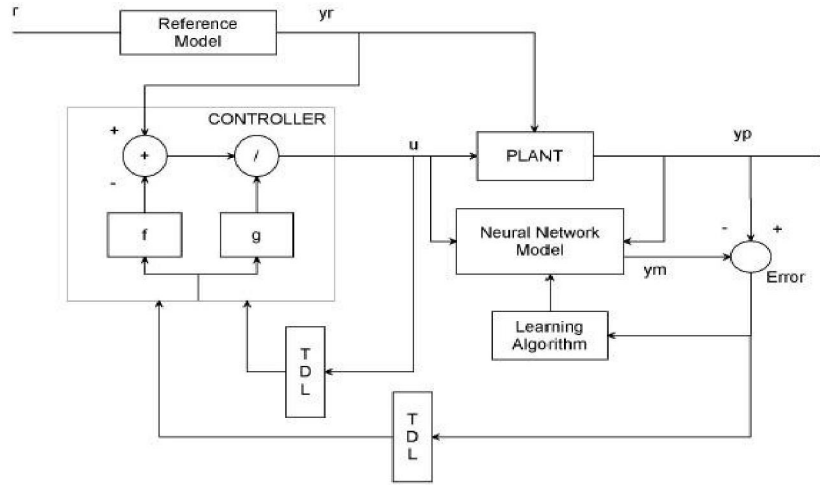


Fig. 5. The process of training model predictive control

The neural network plant model uses preceding inputs and former plant outputs to be expecting destiny values of the plant output. The structure of the neural network plant model is given in Figure 6 below.

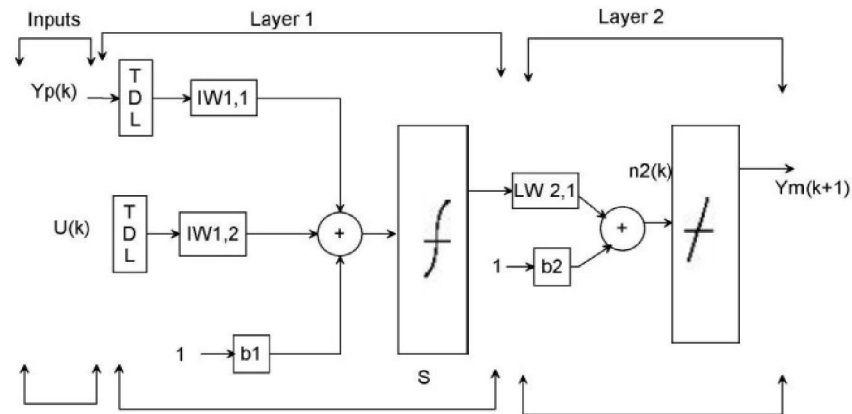


Fig. 6. The structure of the neural network plant model

2) *Predictive Control:*

The model predictive control technique is based totally on the receding horizon method. The neural network model predicts the plant reaction over a

unique time horizon. The predictions are used by a numerical optimization software to decide the control signal that minimizes the following performance criterion over the required horizon.

$$J = \sum_{j=N_1}^{N_2} (y_r(k+j) - y_m(k+j))^2 + \rho \sum_{j=1}^{N_u} (u'(k+j-1) - u'(k+j-2))^2 \quad (8)$$

Where N1, N2, and Nu define the horizons over which the tracking blunders and the manage increments are evaluated. The u' variable is the tentative control signal, yr is the preferred response, and ym is the network model reaction. The cost

determines the contribution that the sum of the squares of the control increments has on the performance index.

The following block diagram illustrates the model predictive control method. The controller

consists of the neural network plant model and the optimization block. The optimization block

determines the values of  $u'$  that limit  $J$ , after which the top of the line  $u$  is input to the plant.

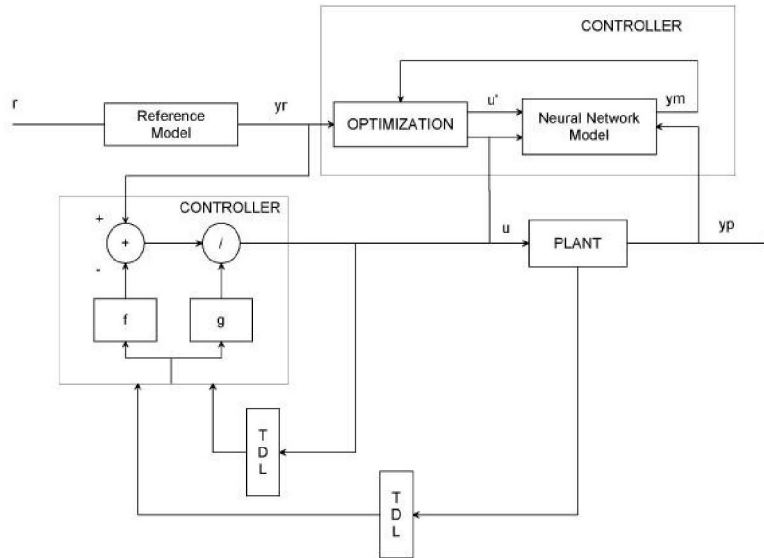


Fig. 7. Block diagram of the model predictive control process

*D. Design of NARMA-L2 Model Controller Using Adaptive Control*

The NARMA-L2 based neural model reference adaptive control structure uses neural networks: a controller network and a plant model network, as

shown in Figure 8 below. The plant model is identified first, and then the controller is trained in order that the plant output follows the reference model output.

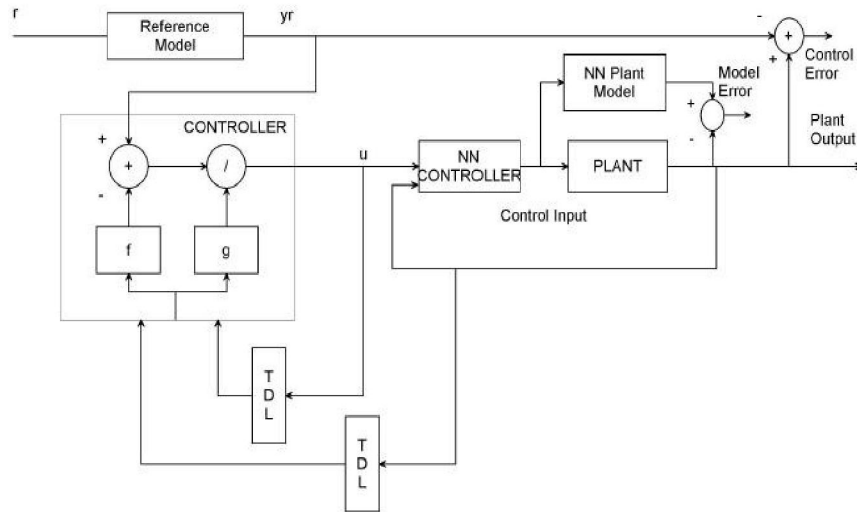


Fig. 8. Block diagram of controller network and a plant model network

Figure 9 indicates the info of the neural network plant model and the neural network controller. Each network has two layers, and you can pick out the quantity of neurons to use within the hidden layers. There are three units of controller inputs:

- Delayed reference inputs

- Delayed controller outputs
- Delayed plant outputs

For each of those inputs, you can select the variety of delayed values to apply. Typically, the variety of delays increases with the order of the plant.

There are two sets of inputs to the neural network plant model: Delayed controller outputs

- Delayed plant outputs

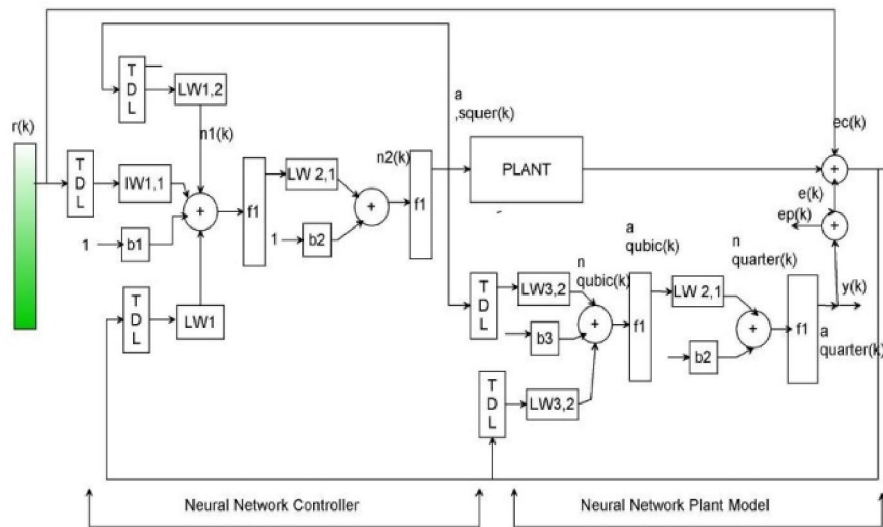


Fig. 9. The neural network plant model and the neural network controller

### III. Result And Discussion

This chapter basically focuses on the comparison of neural network controller with NARMA-L2 model, neural network controller with NARMA-L2 model system identification based predictive controller and neural network controller with NARMA-L2 model based model reference adaptive control. These three systems input is the desired arm position and they generate impulse voltage signal to be given to the arm and the arm deliver arm output position. These three

systems tested with step, sine wave and random desired arm position signal.

#### A. Comparison of the Proposed Controllers using step input signal

The Simulink model for the comparison of neural network controller with NARMA-L2 model, neural network controller with NARMA-L2 model system identification based predictive controller and neural network controller with NARMA-L2 model based model reference adaptive control using step input signal is shown in the Figure 10 below.

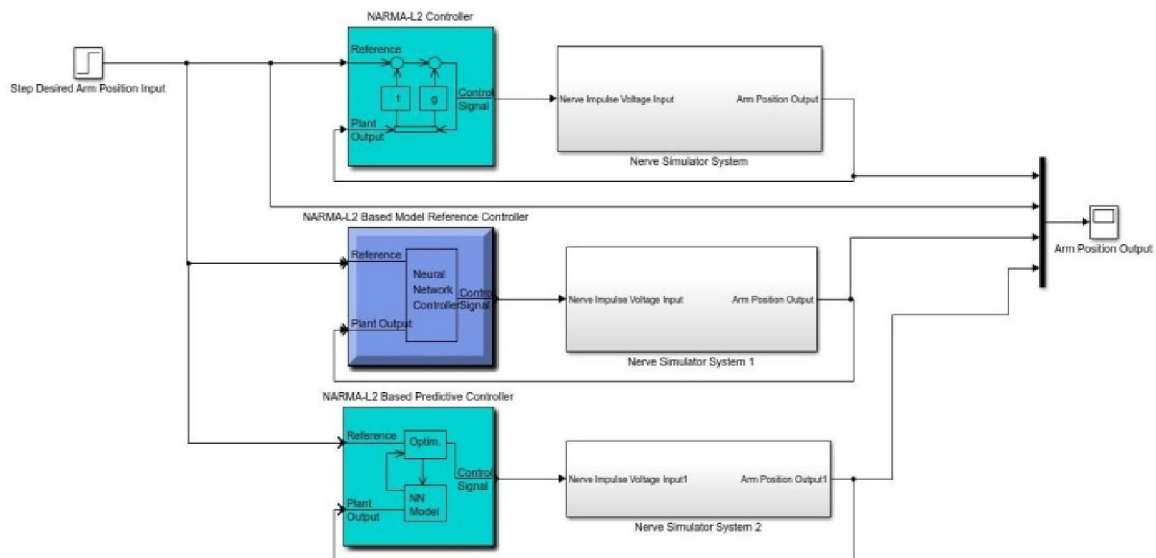


Fig. 10. Step response Simulink model

The simulation output for the comparison of the neural network controller with NARMA-L2 model, neural network controller with NARMA-L2 model system identification based predictive controller and

neural network controller with NARMA-L2 model based model reference adaptive control using step input signal is shown in the Figure 11 below.

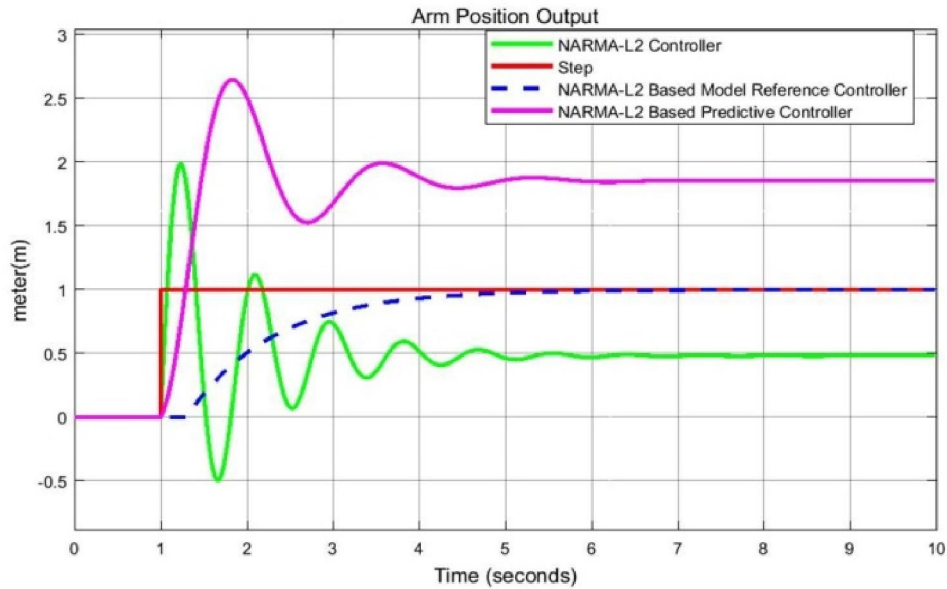


Fig. 11. Step response simulation result

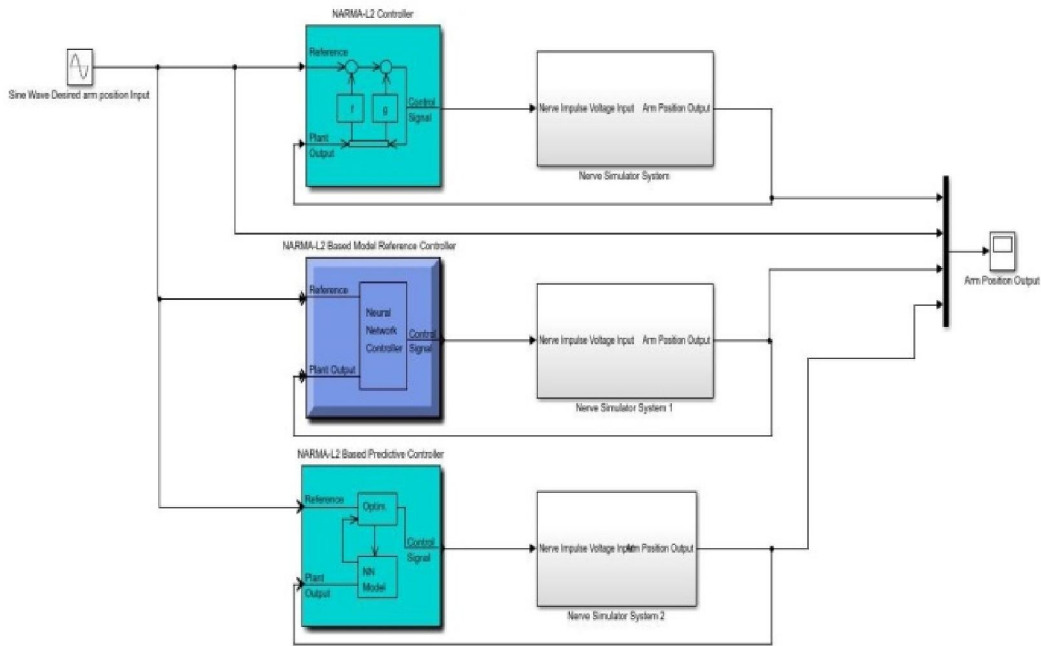


Fig. 12. Sine wave response Simulink model

The neural network controller with NARMA-L2 controller has a high percentage overshoot and since the step input signal is the desired arm position of the patient and the output of this controller has a steady state value of 0.5 m while the desired arm position is 1m. This show us that the neural network controller

with NARMA-L2 controller does not feed enough nerve impulse voltage to the nerve of the arm. The neural network controller with NARMA-L2 model system identification based predictive controller has a bigger percentage overshoot and since the step input signal is the desired arm position of the patient and the



output of this controller has a steady state value of 1.75 m while the desired arm position is 1m. This show us that the neural network controller with NARMA-L2 model system identification based predictive controller feed excess nerve impulse voltage to the nerve of the arm. The neural network controller with NARMA-L2 model based model reference adaptive control has a no percentage overshoot and since the step input signal is the desired arm position of the patient and the output of this controller has the same steady state value of 1 m with the desired arm position. This show us that the neural network controller with NARMA-L2 model based model reference adaptive control gives the exact nerve impulse voltage to the nerve of the arm.

### B. Comparison of the Proposed Controllers using Sine Wave Input Signal

The Simulink model for the comparison of neural network controller with NARMA-L2 model, neural network controller with NARMA-L2 model system identification based predictive controller and neural network controller with NARMA-L2 model based model reference adaptive control using sine wave input signal is shown in the Figure 12.

The simulation output for the comparison of the neural network controller with NARMA-L2 model, neural network controller with NARMA-L2 model system identification based predictive controller and neural network controller with NARMA-L2 model based model reference adaptive control using sine wave input signal is shown in the Figure 13 bellow.

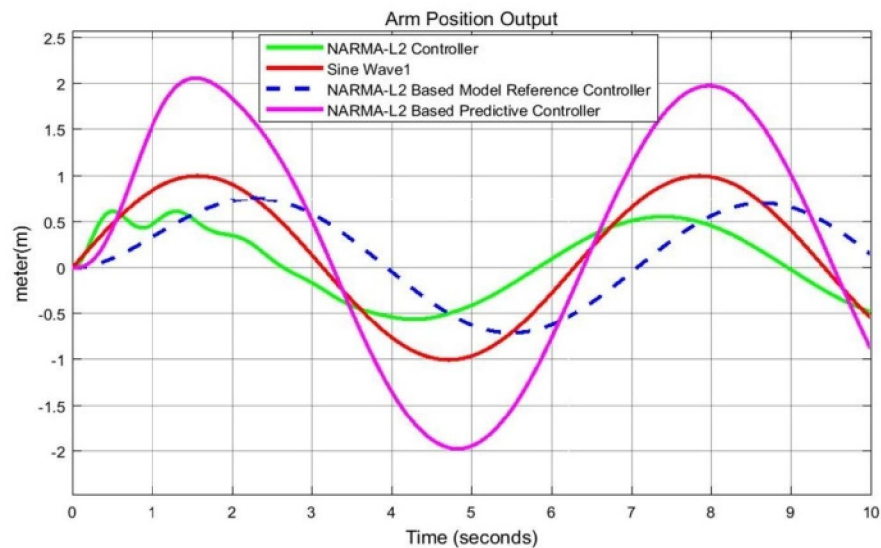


Fig. 13. Sine wave response simulation result

The neural network controller with NARMA-L2 controller sine wave input signal is the desired arm position of the patient and the output of this controller has a peak value of 0.6 m while the desired arm position is 1m. This show us that the neural network controller with NARMA-L2 controller gives low impulse voltage to the nerve of the arm. The neural network controller with NARMA-L2 model system identification based predictive controller sine wave input signal is the desired arm position of the patient and the output of this controller has a peak value of 2.1 m while the desired arm position is 1m. This show us that the neural network controller with NARMA-L2 model system identification based predictive controller feed excess nerve impulse voltage to the nerve of the arm. The neural network controller with NARMA-L2 model based model reference adaptive

control sine wave input signal is the desired arm position of the patient and the output of this controller has a peak value of 0.8 m while the desired arm position is 1m. This show us that the neural network controller with NARMA-L2 model based model reference adaptive control gives almost the exact nerve impulse voltage to the nerve of the arm.

### C. Comparison of the Proposed Controllers using Random Input Signal

The Simulink model for the comparison of neural network controller with NARMA-L2 model, neural network controller with NARMA-L2 model system identification based predictive controller and neural network controller with NARMA-L2 model based model reference adaptive control using random input signal is shown in the Figure 14 bellow.

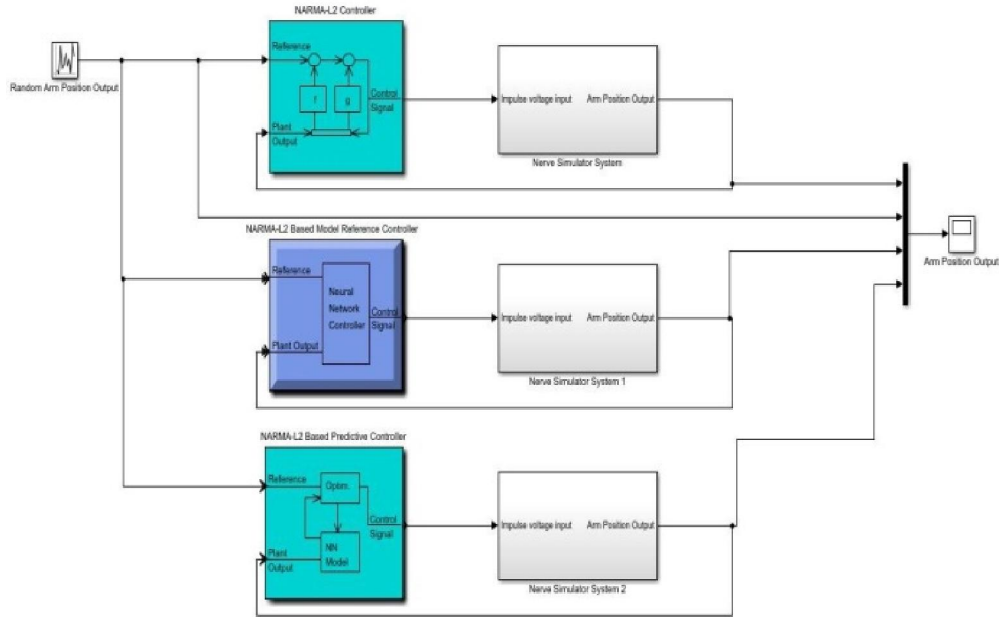


Fig. 14. Random input response Simulink model

The simulation output for the comparison of the neural network controller with NARMA-L2 model, neural network controller with NARMA-L2 model system identification based predictive controller and

neural network controller with NARMA-L2 model based model reference adaptive control using random input signal is shown in the Figure 15 bellow.

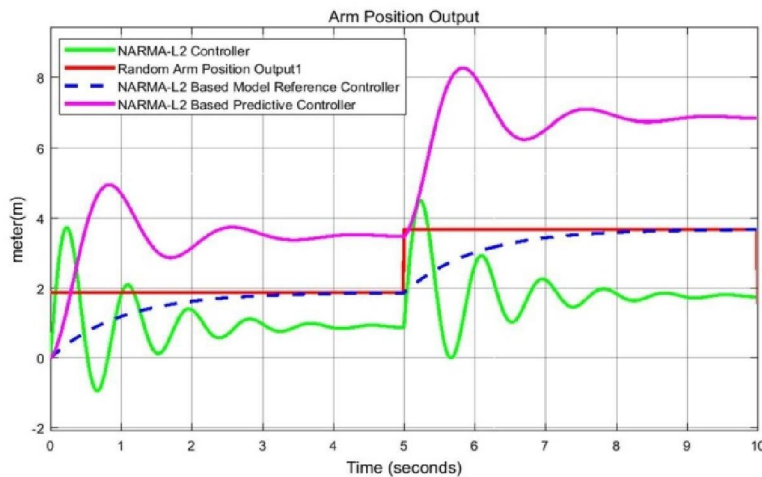


Fig. 15. Random input response simulation result

The neural network controller with NARMA-L2 controller random input signal is the desired arm position of the patient and the output of this controller has a peak value of 4.4 m while the desired arm position is 3.5m. This show us that the neural network controller with NARMA-L2 controller gives high impulse voltage to the nerve of the arm. The neural network controller with NARMA-L2 model system identification based predictive controller random input signal is the desired arm position of the patient and the output of this controller has a peak value of 8.5 m

while the desired arm position is 3.5 m. This show us that the neural network controller with NARMA-L2 model system identification based predictive controller feed excess nerve impulse voltage to the nerve of the arm. The neural network controller with NARMA-L2 model based model reference adaptive control random input signal is the desired arm position of the patient and the output of this controller has a peak value of 3.5 m while the desired arm position is 3.5 m. This show us that the neural network controller with NARMA-L2 model based model reference

adaptive control gives the exact nerve impulse voltage to the nerve of the arm.

#### D. Numerical Value Comparison of the proposed systems

The numerical value comparison of the proposed systems is shown in the Table 1 below.

Table I Numerical Value Comparison Of The Proposed Systems

No	System	Step	Sine wave	Random
1	Desired Arm Position	1	1	3.5
2	NARMA-L2 model	0.5	0.6	4.4
3	Model reference	1	0.8	3.5
4	Predictive controller	1.75	2.1	8.5

The result from Table 1 shows us that the neural network controller with NARMA-L2 model based model reference adaptive control show the best response.

#### IV. Conclusion

In this thesis, nerves system based arm position sensor device is used to measure the exact arm position for nerve patients using the proposed systems. Three different systems are proposed which are a neural network controller is designed with NARMA-L2 model, neural network controller is designed with NARMA-L2 model system identification based predictive controller and neural network controller is designed with NARMA-L2 model based model reference adaptive control system.

The proposed controllers are tested for comparing the actual and desired arm position of the nerves system based arm position sensor device for three desired arm position inputs (step, sine wave and random).

The simulation result for a step input signals shows that the neural network controller with NARMA-L2 controller feeds a high impulse voltage to the nerve of the arm and the neural network controller with NARMA-L2 model system identification based predictive controller feed excess nerve impulse voltage to the nerve of the arm and the neural network controller with NARMA-L2 model based model reference adaptive control gives the exact nerve impulse voltage to the nerve of the arm.

The simulation result for a sine wave input signals shows that the neural network controller with NARMA-L2 controller gives high nerve impulse voltage to the nerve of the arm and the neural network controller with NARMA-L2 model system identification based predictive controller feed excess nerve impulse voltage to the nerve of the arm and the neural network controller with NARMA-L2 model based model reference adaptive control gives the exact nerve impulse voltage to the nerve of the arm.

The simulation result for a random input signals shows that the neural network controller with NARMA-L2 controller gives high nerve impulse

voltage to the nerve of the arm and the neural network controller with NARMA-L2 model system identification based predictive controller feed excess nerve impulse voltage to the nerve of the arm and the neural network controller with NARMA-L2 model based model reference adaptive control gives the exact nerve impulse voltage to the nerve of the arm.

Finally, the comparative simulation result prove the effectiveness of the presented neural network controller with NARMA-L2 model based model reference adaptive control and it achieves to balance between the actual and desired arm position tests for the nerve patient by adjusting the nerve impulse voltage given to the arm.

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