

Fuzzy Logic Controller For An Mobile Robot

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Abstract: In this develops the development of an autonomous wall-following robot is presented. The wall following controller is a two input, two output system. The inputs are two proximity measurements to the wall, and the outputs are the speeds of the two rear wheels. A variety of evolutionary algorithms, operating according to Darwinian concepts, have been proposed to approximately solve problems of common engineering applications. Increasingly common applications involve automatic learning of nonlinear mappings that govern the behavior of control systems. In many cases where robot control is of primary concern, the systems used to demonstrate the effectiveness of evolutionary algorithms often do not represent practical robotic systems. In this paper, genetic programming (GP) is the evolutionary strategy of interest. It is applied to learn fuzzy control rules for a practical autonomous vehicle steering control problem, namely, path tracking. GP handles the simultaneous evolution of membership functions and rule bases for the fuzzy path tracker.

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1. Introduction

Mobile robots are mechanical devices capable of moving in an environment with a certain degree of autonomy. Autonomous navigation is associated to the availability of external sensors that capture information of the environment through visual images or distance or proximity measurements. The most common sensors are distance sensors (ultrasonic, laser, etc) capable of detecting obstacles and of measuring the distance to walls close to the robot path. When advanced autonomous robots navigate within indoor environments (industrial or civil buildings), they have to be endowed the ability to move through corridors, to follow walls, to turn corners and to enter open areas of the rooms [1,2].

Genetic programming [3] has recently been demonstrated to be a viable approach to learning fuzzy logic rules for mobile robot control and navigation [4, 5]. Herein, we address the simultaneous design of fuzzy logic controllers (FLCs) using GP, i.e. evolution of both the input membership functions and the rule base. In addition, we extend the evolutionary influence of GP by incorporating the random selection of fuzzy logic connectives (t-norms) into the learning process. Finally, we examine the robustness of the evolved controllers by corrupting sensory data used by the path following robot, and by increasing the nominal forward velocity of the vehicle. This provides an indication of how well GP can evolve practical solutions that also retain the tolerance of imprecision and uncertainty characteristic of FLCs.

2. Overviews of Fuzzy Control and GP

The robot that is to be controlled was initially built to take part in an IEEE competition, held at Cleveland State University in 2004. The goal of this competition is to compete head to head on the playing board with an opponent and obtain the most points in an allotted amount of time. The dimensions of the robot had to be within those specified in the competition. The robot had to fit within a 1.5-foot square and could not exceed 1.5 feet in height. It should be totally autonomous, shouldn't transmit or receive signals to or from the outside of the playing area, and shall not be equipped to intentionally harm its opponents. It also shouldn't carry any onboard cameras. The main goal of this work, keeping in mind the requirements of the competition, was to cover as much of the playing area as possible within the shortest time so that the maximum points can be scored. The robot that was built placed second among eleven other competitors from different schools.

3. Types of Robotic Behavior

A mobile robot could be modeled in numerous ways, but the most important factor for defining the model would be the application and the complexity involved. The mobile robot designed in this work is a wheeled robot intended for indoor use as opposed to other types (legged, airborne, and submersible mobile robots). This robot type is the easiest to model, control, and build. There are various behaviors that could be modeled, like wall following, collision avoidance, corridor following, goal seeking, adaptive goal seeking, etc. With the competition in mind we had thought of implementing a wall following robot. This

robot would follow the boundaries of the playing area and cover a maximum area in a predefined path programmed into its onboard microcontroller.

Various control techniques have been proposed and are being researched. The control strategies of mobile robots can be divided into open loop and closed loop feedback strategies. In open loop control, the inputs to the mobile robots (velocities or torques) are calculated beforehand, from the knowledge of the initial and end position and of the desired path between them in the case of path following. This strategy cannot compensate for disturbances and model errors.

These functions assign a numerical degree of membership to a crisp (precise) number. More precisely, over a given universe of discourse (relevant numerical range) X , the membership function of a fuzzy set, denoted by $\mu(x)$, maps elements $x \in X$ into a numerical value in the closed unit interval, i.e. $\mu(x): X \rightarrow [0, 1]$.

Implementation of a fuzzy controller requires assigning membership functions for inputs and outputs. Inputs to a fuzzy controller are usually measured variables, associated with the state of the controlled plant, that are fuzzified (assigned membership values) before being processed by an inference engine. The heart of the controller inference engine is a set of *if-then* rules whose antecedents and consequences are made up of linguistic variables and associated fuzzy membership functions. Consequences from fired rules are numerically aggregated by fuzzy set union and then collapsed (defuzzified) to yield a single crisp output as the control signal for the plant. For detailed introductions to fuzzy control, fuzzy set operations, and concepts of fuzzification, inference, aggregation, and defuzzification see one of [2, 6].

In the GP paradigm, a population is comprised of computer programs or procedures (individuals) that are candidate solutions to a particular problem. These individuals participate in a simulated evolution process wherein the population evolves over time in response to selective pressure induced by the relative fitness of individuals in the problem domain. In our approach, each program executes condition-action statements, which collectively serve as a rule base to be embedded in a fuzzy controller. To preserve diversity among populations and vital genetic information among individuals, genetic operators are applied to create new individuals for succeeding generations. When the algorithm finally converges or satisfies its termination criteria, it is anticipated that the best (most fit) individual will be representative of an optimum or near optimum solution.

In the next section, we introduce the autonomous vehicle control problem, followed by discussion of FLC design issues to be considered when employing GP.

1. Literature review

The position error is taken as the deviation of the center of gravity, C , or any other desired point of the robot from the nearest point on the path. The orientation error is the angular deviation of the robot from the tangent of the desired path. Hemami et al derived a state-space kinematic model for this robot where the state vector was comprised of the pose errors described. The reader is referred to either of [7] or [8] for details of the model derivation, which culminates in the following:

$$\begin{bmatrix} \dot{\varepsilon}_d \\ \dot{\varepsilon}_\theta \end{bmatrix} = \begin{bmatrix} 0 & V_u \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \varepsilon_d \\ \varepsilon_\theta \end{bmatrix} + \begin{bmatrix} MC/MP \\ 1/MP \end{bmatrix} V_u \tan \delta \pm \begin{bmatrix} \dot{\eta}_d \\ \dot{\eta}_\theta \end{bmatrix} \quad (1)$$

where V_u is forward linear velocity of the robot, and $\dot{\eta}_d$ and $\dot{\eta}_\theta$ are rates of change of the effects of path curvature. In [8] it is concluded (based on dynamic analysis of the same vehicle) that for small steering angle, $(\tan \delta \cong \delta)$, Equation (1) approximates the slow dynamics of the vehicle when its forward velocity is low. For simulations presented later, we have simplified the robot kinematic model by taking this small steering angle approximation into account. Furthermore, we apply the controller to straight-line path following and, therefore, neglect the model effects of path curvature. Such a simplification does not preclude autonomous tracking of reasonably complicated paths since multi-segment paths can be defined to be piecewise linear.

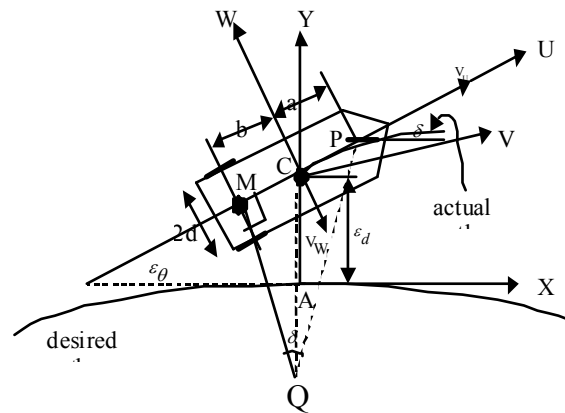


Figure 1. Tracking control and error variables.

For our application, we assume that the robot has dead-reckoning/odometry sensors that provide access to the error states at all times, or permit calculations thereof. This sensory input data is then mapped to control outputs according to the desired control policy. In path following simulations the state vector of the kinematic model is updated using the well-known

fourth-order Runge-Kutta numerical integration method.

The path tracker to be learned by GP is a two-input, single-output fuzzy controller that will map the error states into a proper steering angle at each time step. A population of candidate solutions is created from which a solution will emerge. The allowance for rule bases of various sizes enhances the diversity of the population. That is, the GP system creates individuals in the initial population that each have possibly different numbers of rules within a range (15-30) specified before a run. In the process of learning fuzzy control rules and membership functions, GP manipulates the linguistic variables directly associated with the controller. Given a desired motion behavior, the search space is contained in the set of all possible rule bases that can be composed recursively from a set of functions and a set of terminals. The function set consists of membership function definitions (describing controller inputs), components of the generic fuzzy *if-then* rule, and common fuzzy logic connectives. More specifically, these include functions for fuzzy sets, rule antecedents and consequents, fuzzy set intersection and union, and fuzzy inference. The terminal set is made up of the input and output linguistic variables and the corresponding membership functions associated with the problem.

Each rule base in the current population is evaluated to determine its fitness value for steering the robot from initial locations near the desired path to final locations on the path such that steady state and final pose errors are minimized. This evaluation involves frequent simulation of the robot's motion from each of a finite number of initial conditions until either the goal state is achieved or the allotted time expires. The initial conditions are referred to as *fitness cases* in the GP community. For this problem we use eight different initial conditions, which is a logical choice given the pair-wise symmetry of the possible error categories illustrated in Figure 2. Consider error category (d), which represents a case where the robot is located on the left of the desired path with a negative heading orientation. There also exists a symmetric case where the robot is located on the right of the desired path with a positive heading orientation. These symmetric cases are each represented by error category (a), (b) and (c) illustrated in the figure, yielding a total of eight fitness cases that fully describe the possible combinations of errors with respect to the path.

The fitness function is a measure of performance used to rank each individual relative to others in the population. We compute path tracking performance by summing the Euclidean norms (normalized) of the final error states plus the average control effort ($\bar{\delta}$)

over all eight fitness cases. Thus, the following fitness function drives the evolution process

$$Raw\ Fitness = \sum_{i=1}^8 \sqrt{(\varepsilon_d^2 + \varepsilon_\theta^2 + \bar{\delta}^2)}_i \quad (2)$$

where ε_d and ε_θ are the position error and orientation error existing at the end of each fitness case simulation. The objective of this fitness function is to minimize final path tracking errors as well as the control effort expended. As such, a perfect fitness score is zero and, in general, lower fitness values are associated with better controllers. Simulations thus far showed that including $\bar{\delta}$ as part of the path tracking metric significantly reduces undesired steering oscillations. Fitness functions based solely on final error states sometimes yielded impractical controllers that exhibited rapid oscillations in the steering control signal, which would cause damage to the steering mechanism of a real mobile robot.

The path tracking success of an individual in the population is also based on its ability to minimize tracking errors to within the following specified tolerances, $|\varepsilon_d| < 0.15m$ and $|\varepsilon_\theta| < 0.26\ rad.$, for each fitness case. A fitness case simulation in which these tolerances are satisfied is considered a hit, or successful trial. Thus, each individual has the potential of receiving a total of eight hits during fitness evaluation.

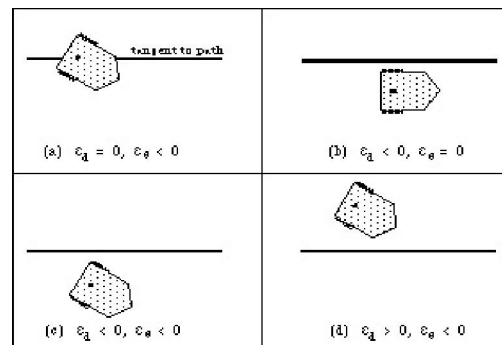


Figure 2. Error categories for control problem.

2. Results

In this section, we present representative results of simulated path tracking performance for an evolved controller. The simulated robot is based on Hemami's kinematic model with dimensions taken from the Hero-1 mobile robot. The Hero-1 has a tricycle wheel configuration in which the front wheel is driven by a DC motor and steered by a stepper motor. Its two rear wheels are passive. Dimensions employed are 0.3m for the wheelbase, and 0.2m for the offset from the rear

axle to the front wheel. These dimensions correspond to the constant lengths $2d$ and MP of Figure 1, respectively. All simulations were conducted assuming a controller sampling rate of 20 Hz and run for a maximum of ten seconds. In each case, the robot travels at a constant nominal forward speed of 1.5 m/s unless otherwise stated.

The GP system was implemented in the C programming language on a 260 MHz MIPS DEC station. Five consecutive runs (initialized using different random number generator seeds) were executed on a population of 200 individuals for a maximum of 50 generations. About one hour of computation time is required for a run of this magnitude. A rule base of 25 rules emerged as the fittest among all five runs. This rule base used five conjunctive rules, three employing the Mamdani t-norm and two employing the Larsen t-norm. The evolved input membership functions associated with the best rule base are shown in Figure 3 and the rules are listed in Table 1. The notations NB , NS , Z , PS , and PB represent fuzzy linguistic terms of “negative big”, “negative small”, “zero”, “positive small”, and “positive big”, respectively. Terms describing the inputs, ϵ_d and ϵ_θ , are preceded with the prefix “p” and “o” respectively. The fixed output membership functions are shown in Figure 4, where the linguistic terms are labeled without prefixes.

The evolved controller received a raw fitness of 0.1091 with 8 hits. In [4], an FLC designed manually, through a lengthy process of trial-and-error, was presented which also used 25 rules. Hours of iterative refinement of membership functions and rules were invested before arriving at a suitable design. In comparison, the hand-derived FLC received a comparable raw fitness (0.08 with 8 hits) for the identical tracking problem. Figure 5 shows the temporal responses of position error, orientation error, and control effort for the evolved controller and for the hand-derived controller. This result corresponds to error category (d) of Figure 2, with initial conditions of

$\epsilon_d = 0.8$ m and $\epsilon_\theta = -0.9$ rad. In [8] it was shown that this error category is the most general for studying path tracking by tricycle-type vehicles. It is most general in the sense that in the process of correcting vehicle steering from initial states in all other error categories, the vehicle error status ultimately reduces the category (d) of Figure 2 or its counter-pair. In all fitness cases, the evolved controller achieved comparable response characteristics to those of the hand-derived controller using an equivalent number of rules.

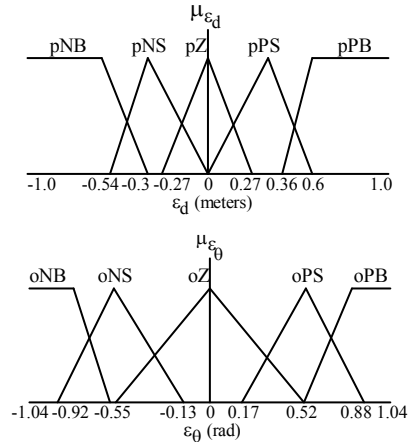


Figure 3. Co-evolved input membership functions.

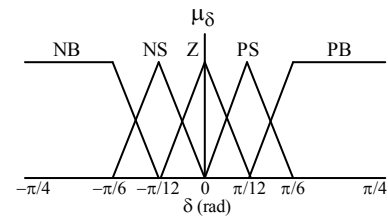


Figure 4. Output membership functions.

TABLE 1. Best Evolved Rule Base

1	IF oZ THEN NS
2	IF pPB THEN Z
3	IF pNB THEN Z
4	IF pPS THEN NB
5	IF pNS and oPS THEN NS (Mamdani's <i>min</i>)
6	IF pNB THEN PB
7	IF oNS THEN Z
8	IF oNB THEN PS
9	IF pNS THEN NS
10	IF pNS and oZ THEN PB (Larsen's <i>prod</i>)
11	IF oPB THEN NB
12	IF pNS and oPB THEN NB (Larsen's <i>prod</i>)
13	IF pPS THEN NS
14	IF oNS THEN PB
15	IF pPB THEN NB
16	IF oZ THEN PS
17	IF oNB THEN PB
18	IF pNS and oNS THEN PB (Mamdani's <i>min</i>)
19	IF pNS THEN Z
20	IF oPS THEN NB
21	IF pZ THEN PS
22	IF pPB and oZ THEN Z (Mamdani's <i>min</i>)
23	IF pPB THEN PS
24	IF oPS THEN PS
25	IF oNS THEN PS

6. Robustness Characteristics

Given the capability to evolve FLCs that can effectively follow paths, an important next step is to examine their robustness to practical perturbations. To test the noise robustness of the evolved controller, simulations were performed with the imposition of a noise signal upon the sensor measurement related to heading (orientation). We assume that the error states are derived from sensor measurements which, due to their imperfect nature, introduce an additive sinusoidal noise signature of small amplitude and low frequency (relative to the controller sampling frequency) that corrupts the orientation error. For this investigation we impose the sensor noise signal, $n(t) = 0.15\cos(3t)$ with $t = kT$, where $k=1,2,3,\dots$ is the sampling instant, and T is the sampling period. Thus, the noise amplitude is bounded by 0.15 radians (10 degrees), and at any sampling instant the corrupted orientation error signal lies in the range of $(\mathcal{E}_\theta \pm 0.15)$ radians.

In addition to the additive noise, we also increased the constant nominal forward speed of the robot by 20%, which resulted in a simulated speed of 1.8m/s. A typical result is shown in Figure 6, which

illustrates the performance of both the evolved controller and the hand-derived controller when induced with noise and an increased vehicle speed. While the oscillatory effects of the added noise are clearly evident in the steady state response, the controller successfully navigates the robot onto the path and maintains the steady state errors within the tolerances specified earlier. Thus, this evolved fuzzy controller exhibits path tracking robustness to the imposed perturbations. This result is representative of temporal responses for each of the remaining fitness cases. In simulations completed thus far, the most robust fuzzy controllers were those evolved when GP was allowed to randomly select t-norms.

The performance assessment of the evolved controller with regard to robustness is based upon the assumption that low frequency oscillations within the control signal of amplitude less than 0.026 radians (1.5 degrees) are practical. In light of this assumption, the results indicate that the evolved FLC was able to navigate the robot along the desired path with the imposed perturbation of sensor noise and the increase in the robot's nominal speed.

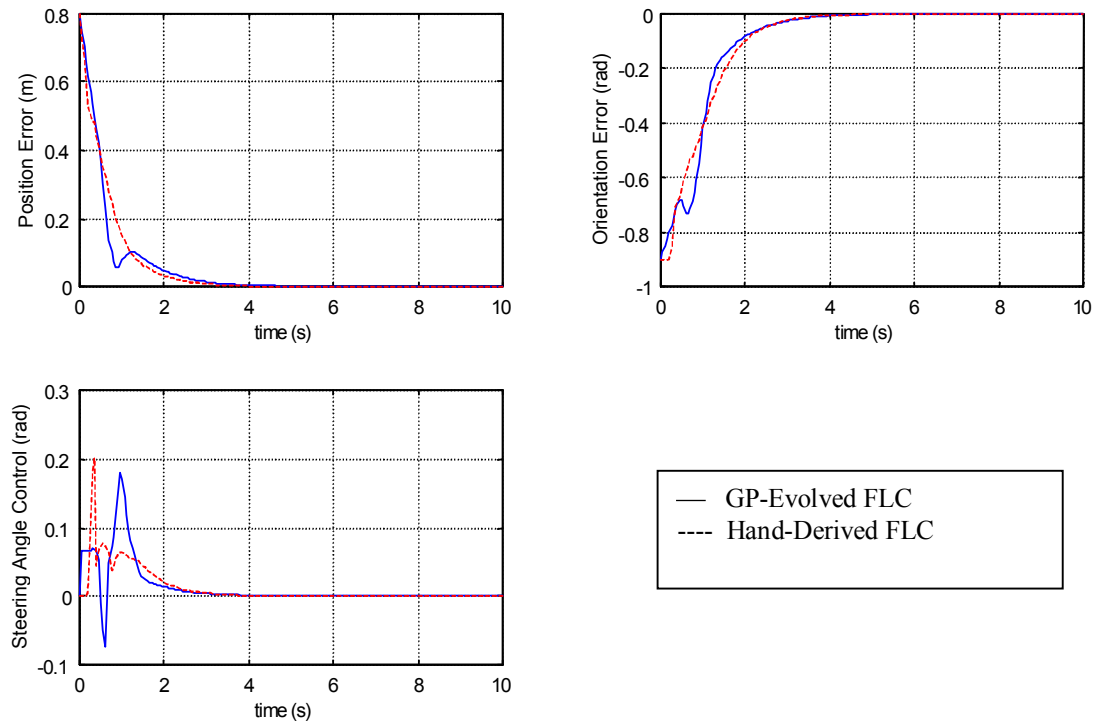


Figure 5. Evolved FLC path tracking performance.

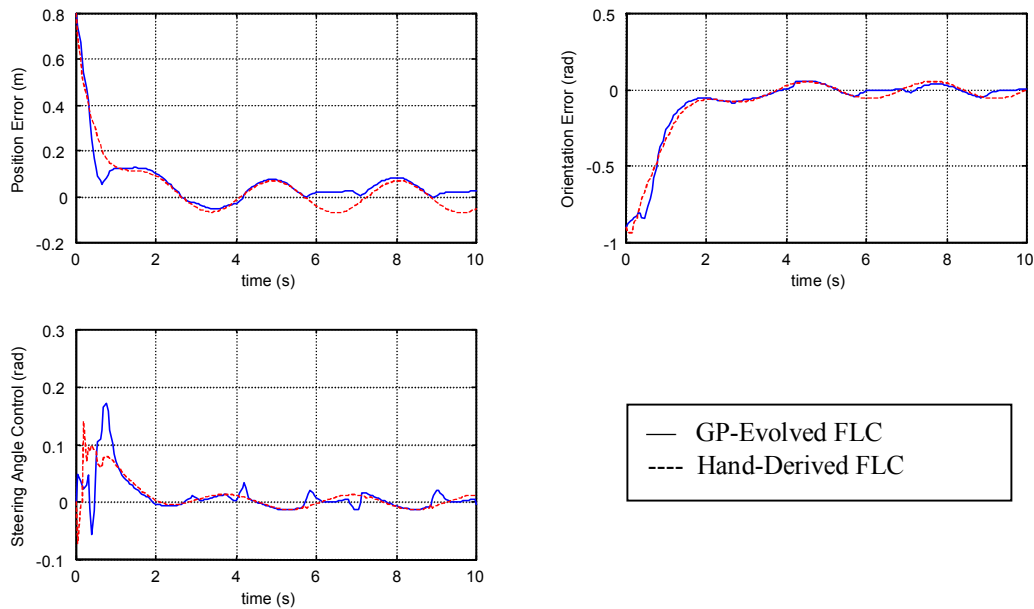


Figure 6. Evolved FLC response to sensor noise and increased forward speed.

7. Conclusions

This paper has demonstrated an approach to path tracking controller design based on soft computing methods. GP was successfully applied to discover fuzzy controllers capable of navigating a mobile robot to track straight-line paths in the plane. The performance of the best-evolved FLC was comparable to that of a manually derived FLC, which required a considerably longer design cycle. GP simultaneously evolved membership functions and rules for an FLC that demonstrated satisfactory responsiveness to various initial conditions while utilizing minimal human interface. The speed of evolution alone serves as a strong basis for practical application of GP in the controller design process. The approach enables expeditious design of FLCs that can be directly applied to a physical system. Alternatively, human experts can use the rapidly evolved FLCs as design starting points for further manual refinement. Finally, the evolved FLC was shown to be robust to perturbations of sensor noise and an increase in nominal robot speed. This supports the notion that genetically evolved FLCs can have practical utility.

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