**Advanced theory on Dust grain orbiting the sun**

 Manjunath. R. (Reader in physics)

 #16, 8th Main road,

 Shivanagar, Rajajinagar,

 Bangalore-560010

 Karnataka, India

 **manjunathr1988@yahoo.in**

**Abstract** :The new mathematical model allows to calculate Poynting–Robertson force . It is shown that the equation for the calculation ofPoynting–Robertson force accounts for the force exerted by incoming solar radiation,gravitational radius of sun and dust grain's orbital radius.The equation **FPR = F \* (Rg /2R )^1/2 (FPR =** Poynting–Robertson force , **F**= Force exerted by solar radiation , **Rg=** gravitational radius of sun, **C** is the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) in vaccum , **R** is the dust grain's orbital radius) was developed based on the Newton gravitational concepts , classical mechanical concepts and basic concepts of physics.The calculation of wavelength of incoming solar radiation accounts the dust grain's orbital radius and dust grain’s radius.The energy flux of incoming solar radiation ,momentum of solar radiation,sun’s radius and dust grain's orbital radius are brought togather in one frame of reference .

**Key words :** Poynting–Robertson force , Solar radiation, wavelength, speed of light ,Energy flux ........

 Power of radiation can be given by **P=hf^2 i.e P= (hf)c/ λ** (1)

 Force exerted by radiation can be given by **F=hf/ λ**

Proof for **F=hf/ λ** :

#  Determination of the Photon Force and Pressure

 [Reissig, Sergej](http://adsabs.harvard.edu/cgi-bin/author_form?author=Reissig,+S&fullauthor=Reissig,%20Sergej&charset=UTF-8&db_key=PHY)

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In [1] the formula for the practical determination of the power of a light particle was derived: P = hf^2 (W) (1). For the praxis it is very usefully to define the forces and pressure of the electromagnetic or high temperature heat radiation. The use of the impulse equation F = fracdPdt = fracd(mc)dt (2) together with the Einstein formula for E = mc^2 leads to the following relationship: F = frac1cfracd(mc^2 )dt = frac1cfracdEdt (3) In [1] was shown: - fracdEdt = P (4). With the use the eq. (1), (3), (4) the force value could be finally determinated: | F | = frachf^2 c or | F | = frachcλ ^2 = fracEλ [N]. The pressure of the photon could be calculated with using of the force value and effective area: p = fracFA [Pa]. References 1. About the calculation of the photon power. S. Reissig, APS four corners meeting, Arizona, 2003 -www.eps.org/aps/meet/4CF03/baps/abs/S150020.html

 **E=F λ**

According to Planck’s theory of radiation

 Energy associated with radiation can be given by

 **E=hf**

Thus the equation **E=F λ** becomes **F=hf/ λ**

Then the equation (1) becomes **P=FC** (2)

Here **P=** Power of radiation, **F**= Force exerted by radiation ,**C**= speed of light in vaccum , **h** = planck’sconstant , ***f*=**frequencyof radiation , **λ =** wavelength of radiation .

Consider a dust grain orbiting the sun in the solar system . Newton's law of universal gravitation states that “Every massive particle in the universe attracts every other massive particle with a force which is directly proportional to the product of their masses and inversely proportional to the square of the distance between them “.

 Gravitational force of sun experienced by the dust grains orbiting the sun can be given by

 **FS= GMS m /R^2** (3) Here **F** = Gravitational force between thesun and dust grain, **G** = Universal gravitational constant , **Ms**= Mass of the sun, **m** = Mass of the dustgrain, **R** = Distance between the Sun and dust grain(orbital radius of dust grain).

 Centrifugal force is an outward [force](http://en.wikipedia.org/wiki/Force) associated with curved motion, that is, [rotation](http://en.wikipedia.org/wiki/Rotation) about some (possibly not stationary) center. Centrifugal force is one of several so-called [pseudo-forces](http://en.wikipedia.org/wiki/Pseudo-force) (also known as [inertial forces](http://en.wikipedia.org/wiki/Inertial_force)). Centrifugal force acts on dust grain to prevent the collapse of dust grain towards the sun can be given by

 **Fc= mv^2 /R**  (4)Here  **Fc** = centrifugal force , **m** = Mass of the dustgrain ,**R** = Distance between the Sun and dust grain(orbital radius of dust grain) , **v**= velocity of dust grain .

 By the comparison of (3) and (4)we get

 **R**= **GMS /v^2**  (5)Here **Ms**= Mass of the sun, **R** = Distance between the Sun and dust grain(orbital radius of dust grain), **v**= velocity of dust grain, **G** = Universal gravitational constant .

[Solar radiation](http://en.wikipedia.org/wiki/Solar_radiation) causes a dust grain in the [solar system](http://en.wikipedia.org/wiki/Solar_system) to slowly spiral inward. The drag is essentially a component of [radiation pressure](http://en.wikipedia.org/wiki/Radiation_pressure) tangential to the grain's motion. The first description of this effect, given by Poynting in 1903. The grain of dust circling the Sun (panel (a) of the figure), the Sun's radiation appears to be coming from a slightly forward direction ([aberration of light](http://en.wikipedia.org/wiki/Aberration_of_light)). Therefore the absorption of this radiation leads to a [force](http://en.wikipedia.org/wiki/Radiation_pressure) with a component against the direction of movement. (The angle of aberration is extremely small since the radiation is moving at the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) while the dust grain is moving many orders of magnitude slower than that.)

 

The Poynting–Robertson drag can be understood as an effective force opposite the direction of the dust grain's orbital motion, leading to a drop in the grain's angular momentum. It should be mentioned that while the dust grain thus spirals slowly into the Sun, its [orbital speed](http://en.wikipedia.org/wiki/Orbital_speed) increases continuously.

 Poynting–Robertson force can be given by

 **FPR = Pv/C^2** (6) Here**P** is the power of the incoming solar radiation, **v** is the grain's velocity**, C** is the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) in vaccum, and **R** isthe dust grain's orbital radius , **FPR =** Poynting–Robertson force .

From (1) we know that power of incoming solar radiation can be denoted by  **P=FC**

Then the equation (6) becomes **FPR = (FC )v/C^2**

 **FPR = (Fv) / C** (7) Here **FPR =** Poynting–Robertson force , **F**= Force exerted by solar radiation , **v** is the grain's velocity , **C** is the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) in vaccum **.**

Squaring the equation (7) we get

 **FPR ^2= F^2 \*(v/ C) ^2** (8)

 From (5) we have **R**= **GMS /v^2** i.e  **v^2=**  **GMS / R**

Thus the equation (8) becomes **FPR ^2= F^2 \*(v^2/C ^2)** i.e **FPR ^2= F^2 \*(GMS/RC^2) .**

The Schwarzschild radius (sometimes historically referred to as the gravitational radius) is a characteristic [radius](http://en.wikipedia.org/wiki/Radius) associated with every quantity of [mass](http://en.wikipedia.org/wiki/Mass). Gravitational radiusof the sun can be given by

 **Rg=2 GMS/C^2** (9)

From (9) the equation **FPR ^2= F^2 \*(GMS/RC^2)** can be written as

 **FPR ^2=( F^2\* Rg) /2R** (10)

 **FPR = F \* (Rg /2R )^1/2** (11)

Here **FPR =** Poynting–Robertson force , **F**= Force exerted by solar radiation , **Rg=** gravitational radius of sun, **C** is the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) in vaccum , **R** is the dust grain's orbital radius .

Poynting–Robertson force can also be given by

 **FPR = r^2 /4C^2 \*( GMSLS^2/R^5) ^1/2** (12) Here **C** is the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) in vaccum, **r =** dust grain’s radius, **G** is the universal [gravitational constant](http://en.wikipedia.org/wiki/Gravitational_constant), **Ms** the [Sun](http://en.wikipedia.org/wiki/Sun)'s mass, **Ls** is the solar luminosity and **R** the grain's orbital radius .

 Squaring the (12) we get **FPR^2 = r^4 /16C^4 \*( GMSLS^2/R^5)** (13)

By rearranging (13) we get **FPR^2 = (r^4 /16C^2 )\*( GMS /c^2) \*(LS^2/R^5)** (14)

Gravitational radiusof the sun can be given by **Rg=2 GMS/C^2** then (14) becomes

 **FPR^2 = (r^4 /16C^2 )\*( Rg/2) \*(LS^2/R^5)** (15)

 **FPR^2 = (r^4 /16C^2 )\*( RgLS^2 / 2R^5)** (16)

 **FPR^2 = (r^4 RgLs^2/32C^4R^5 )** (17)

 By equating (17) and (10) we get

 **F^2Rg/ 2R** = **(r^4 RgLs^2/32C^4R^5 )** (18)

Luminosity is a [measurement](http://en.wikipedia.org/wiki/Measurement) of brightness, luminosity of the sun can be given by

  **LS=AS σ TS^4** (19)

Here **AS =**Area of sun emitting radiation **, σ =**Stefan’s constant**, TS=**Surface temperature of sun **.**

 Energy of incoming solar radiation can be given by **E= σ TS^4**  (20)

 **F λ = σ TS^4** (21) Here **F =** force exerted by incoming solar radiation **, λ =** wavelength of solar radiation .

 Thus (19) becomes **LS=AS \*(F λ )** (22)

 By the substitution of value (22) in (18) we get

 **λ ^2 =16C^4 R^4/AS^2r^4** (23)

 **λ =4C^2R^2/AS r^2** (24)

 Area of the sun can be given by **AS =4** **ΠRs^2** (25)

 By the substitution of value (25) in (24) we get

 **λ = R^2C^2/Π RS^2 r^2** (26)

 Here **λ =**wavelength ofincoming solar radiation , **R** is the dust grain's orbital radius, **Π** =constant ( 3.14), **C** is the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) in vaccum , **RS=** Sun radius , **r** = dust grain’s radius .

let us assume the shape of dust grain to be a sphere for the purpose of establishment of expression for pressure exerted by incoming solar radiation

 Area of the dust grain can be given by **Ag =4** Π**r^2** , By multiplying the equation (26) by 4

 we get **λ =4 R^2C^2/ RS^2 Ag** (27)

Pressure exerted by incoming solar radiation on dust grain can be given by ***PS =*F/ Ag** (28)

By putting (28) in (27) we get **λ =4 R^2C^2*PS* / RS^2 F** i.e **F λ =4 R^2C^2*Pp*/ RS^2** (29)

 **E= 4 R^2C^2*PS*/ RS^2** (Since **E= F λ )** (30)

 **E / C^2 = 4 R^2*PS*/ RS^2** (31) Energy of incoming solar radiation can be given by **E= mc^2** ,

 Here **m** =Mass of incoming solar radiation

  ***PS* = mRS^2 /4 R^2** (32) Here ***PS=*** Pressure exerted by incoming solar radiation , **m** =mass of incoming solar radiation , **RS=** Sun radius, **R** is the dust grain's orbital radius .

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 The mass equivalent density of radiation density can be given by

 ***Ps*=u/3 i.e u =3Ps**

Here ***Ps*=** Radiation pressure ,**u** = mass equivalent density of radiation

 **u=3 mRS^2 /4 R^2** (34)

Solar radiation pressure can be given by

 **Ps = EF /C**

Here **EF =**Energy flux of solar radiation **,PS =** Solar radiation pressure,**C**=Speed of light in vaccum

 Equation (32) becomes **EF = pRS^2 /4 R^2** (35)

Here **p=**momentum of solar radiation

 **Result :**

1) Poynting–Robertson force can also be given by **FPR = F \* (Rg /2R )^1/2**  **FPR =** Poynting–Robertson force , **F**= Force exerted by solar radiation , **Rg =** gravitational radius of sun, **C** is the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) in vaccum , **R** is the dust grain's orbital radius **.**

 2) The wavelength ofincoming solar radiation can be given by **λ = R^2C^2/Π RS^2 r^2** **λ =**wavelength ofincoming solar radiation , **R** is the dust grain's orbital radius, **Π** =constant ( 3.14), **C** is the [speed of light](http://en.wikipedia.org/wiki/Speed_of_light) in vaccum , **RS=** Sun radius , **r** = dust grain’s radius

3) The mass equivalent density of radiation density can be given by **u=3 mRS^2 /4 R^2 m** =mass of incoming solar radiation , **RS=** Sun radius, **R** is the dust grain's orbital radius , **u** = mass equivalent density of radiation

4) Energy flux of incoming solar radiation can be given by **EF = pRS^2 /4 R^2 p=**momentum of solar radiation , **RS=** Sun radius, **R** is the dust grain's orbital radius , **EF =**Energy flux of sola r radiation .