

**The New Prime theorem (31)**

$$P_1 = P^9 \pm m \quad \text{and} \quad P_1 = (2P)^9 \pm n$$

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jiangchunxuan@vip.sohu.com**Abstract:** Using Jiang function we prove  $P_1 = P^9 \pm m$  and  $P_1 = (2P)^9 \pm n$ .[Chun-Xuan Jiang. **The New Prime theorem(31)**  $P_1 = P^9 \pm m$  and  $P_1 = (2P)^9 \pm n$ . *Academ Arena* 2015;7(1s): 54-56]. (ISSN 1553-992X). <http://www.sciencepub.net/academia>. 31**Keywords:** prime; theorem; function; number; new**Theorem 1.** Let  $m$  be an even number which is not cube and ninth power.

$$P_1 = P^9 + m \quad (m \neq a^3, a^9) \tag{1}$$

For every even number  $m$  there exist infinitely many primes  $P$  such that  $P_1$  is a prime.**Proof.** We have Jiang function [1,2]

$$J_2(\omega) = \prod_P [P-1 - \chi(P)] \tag{2}$$

where  $\omega = \prod_P P$ ,  $\chi(P)$  is the number of solutions of congruence

$$q^{15} + m \equiv 0 \pmod{P}, q = 1, \dots, P-1 \tag{3}$$

We have

$$m^{\frac{P-1}{3}} \equiv 1 \pmod{P} \tag{4}$$

If (4) has a solution then  $\chi(P) = 3$ . If (4) has no solutions then  $\chi(P) = 0$ .

We have

$$m^{\frac{P-1}{9}} \equiv 1 \pmod{P} \tag{5}$$

If (5) has a solution then  $\chi(P) = 9$ . If (5) has no solutions then  $\chi(P) = 0$ .  $\chi(P) = 1$  otherwise. We have

$$J_2(\omega) \neq 0 \tag{6}$$

We prove that (1) has infinitely many primes solutions.

We have asymptotic formula [1,2]

$$\pi_2(N, 2) = |\{P \leq N : P_1 = \text{prime}\}| \sim \frac{J_2(\omega)\omega}{9\phi^2(\omega)} \frac{N}{\log^2 N} \tag{7}$$

In the same way we are able to prove  $P_1 = P^9 - m$ .**Theorem 2.** Let  $n$  be an odd number which is not cube and ninth power.

$$P_1 = (2P)^9 + n \tag{8}$$

has infinitely many prime solutions.

**Proof.** we have Jiang function [1,2]

$$J_2(\omega) = \prod_P [P-1 - \chi(P)] \tag{9}$$

where  $\chi(P)$  is the number of solutions of congruence

$$(2q)^9 + n \equiv 0 \pmod{P}, q = 1, \dots, P-1. \quad (10)$$

We have

$$n^{\frac{P-1}{3}} \equiv 1 \pmod{P} \quad (11)$$

If (11) has a solution then  $\chi(P) = 3$ . If (11) has no solutions then  $\chi(P) = 0$ .

We have

$$n^{\frac{P-1}{9}} \equiv 1 \pmod{P} \quad (12)$$

If (12) has a solution then  $\chi(P) = 9$ . If (12) has no solutions then  $\chi(P) = 0$ .  $\chi(P) = 1$  otherwise.

We have

$$J_2(\omega) \neq 0 \quad (13)$$

We prove that (8) has infinitely many prime solutions.

We have asymptotic formula [1,2]

$$\pi_2(N, 2) = \left| \{P \leq N : P_1 = \text{prime}\} \right| \sim \frac{J_2(\omega)\omega}{9\phi^2(\omega)} \frac{N}{\log^2 N} \quad (14)$$

In the some way we are able to prove  $P_1 = (2P)^9 - n$ .

**Remark.** The prime number theory is basically to count the Jiang function  $J_{n+1}(\omega)$  and Jiang prime  $k$ -tuple

singular series  $\sigma(J) = \frac{J_2(\omega)\omega^{k-1}}{\phi^k(\omega)} = \prod_P \left( 1 - \frac{1 + \chi(P)}{P} \right) \left( 1 - \frac{1}{P} \right)^{-k}$  [1,2], which can count the number of prime

number. The prime distribution is not random. But Hardy prime  $k$ -tuple singular series

$\sigma(H) = \prod_P \left( 1 - \frac{\nu(P)}{P} \right) \left( 1 - \frac{1}{P} \right)^{-k}$  is false [3-8], which cannot count the number of prime numbers.

Szemerdi's theorem does not directly to the primes, because it can not count the number of primes. It is unusable. Cramr's random model cannot prove prime problems. It is incorrect. The probability of  $1/\log N$  of being prime is false. Assuming that the events " $P$  is prime", " $P+2$  is prime" and " $P+4$  is prime" are independent, we conclude that  $P$ ,  $P+2$ ,  $P+4$  are simultaneously prime with probability about  $1/\log^3 N$ .

There are about  $N/\log^3 N$  primes less than  $N$ . Letting  $N \rightarrow \infty$  we obtain the prime conjecture, which is false. The tool of additive prime number theory is basically the Hardy-Littlewood prime tuple conjecture, but can not prove and count any prime problems[6].

*Mathematicians have tried in vain to discover some order in the sequence of prime numbers but we have every reason to believe that there are some mysteries which the human mind will never penetrate.* Leonhard Euler

*It will be another million years, at least, before we understand the primes.* Paul Erdős

我们研究看不见摸不着的素数理论。谁也没研究过的素数理论。

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